



Universitat Autònoma  
de Barcelona

# Failure analysis of MOS devices using spatial statistics

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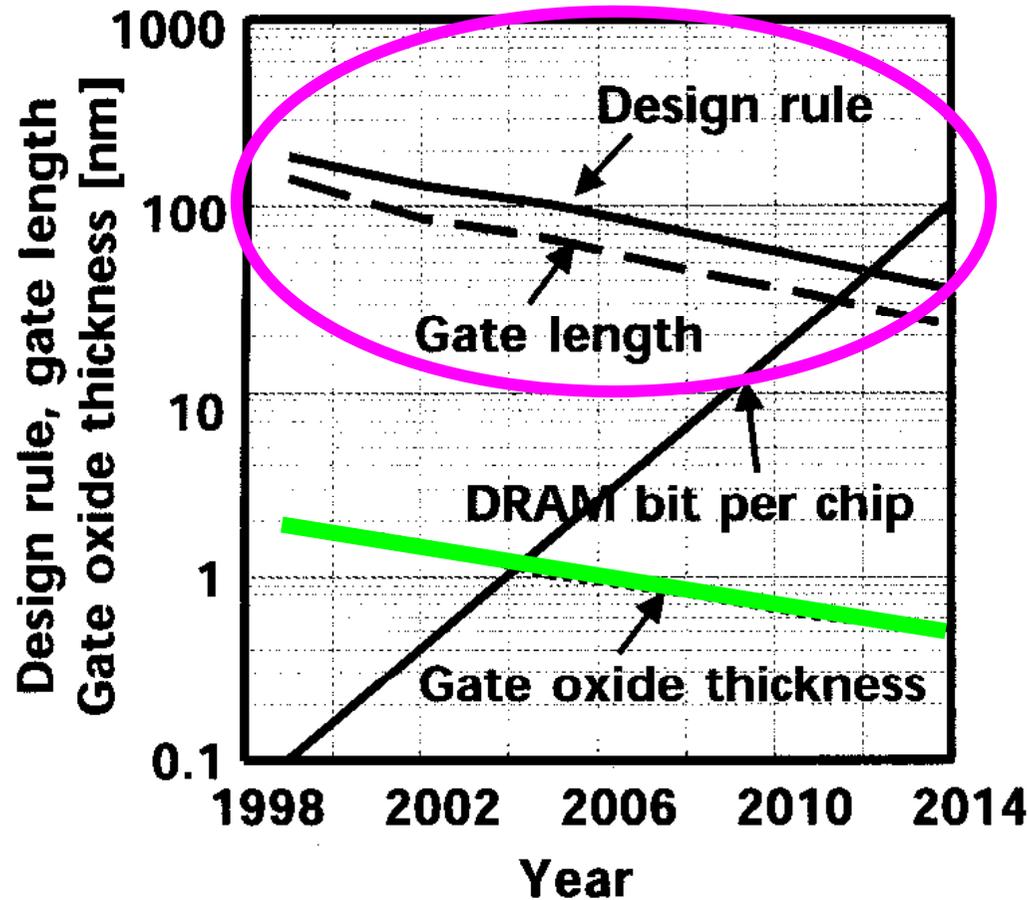
IEEE-EDL Distinguished Lecturer Program

Tokyo Institute of Technology - September 2011

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- Review basic concepts about oxide reliability
- Breakdown spots visualization methods
- Localization methods in 1D and 2D
- Point pattern analysis using spatial statistics
- Application to MOS and MIM devices
- Conclusions

# Scaling rules of MOS devices



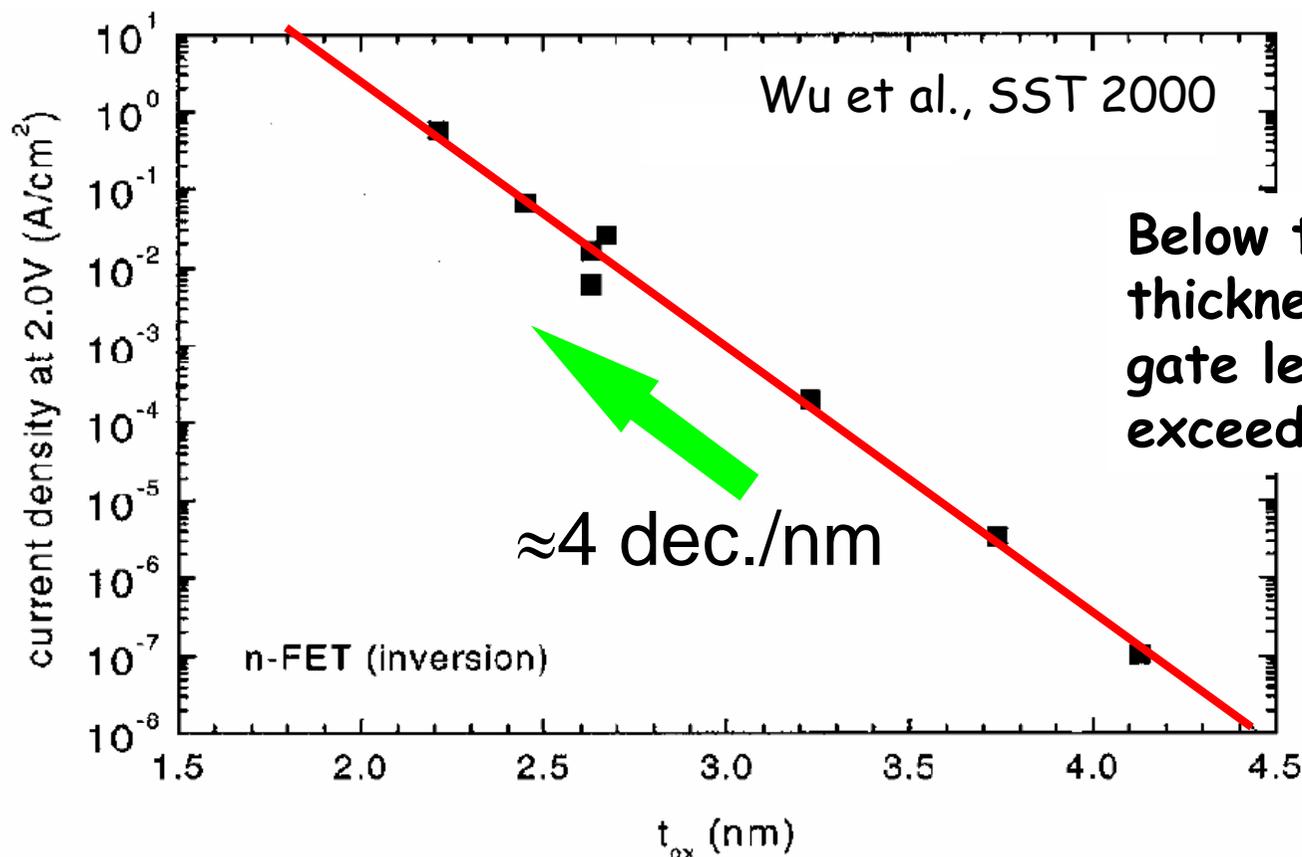
Smaller devices



integration density ↑  
switching speed ↑  
cost per function ↓

**REDUCTION OF THE GATE OXIDE THICKNESS**

# Gate leakage current vs. oxide thickness



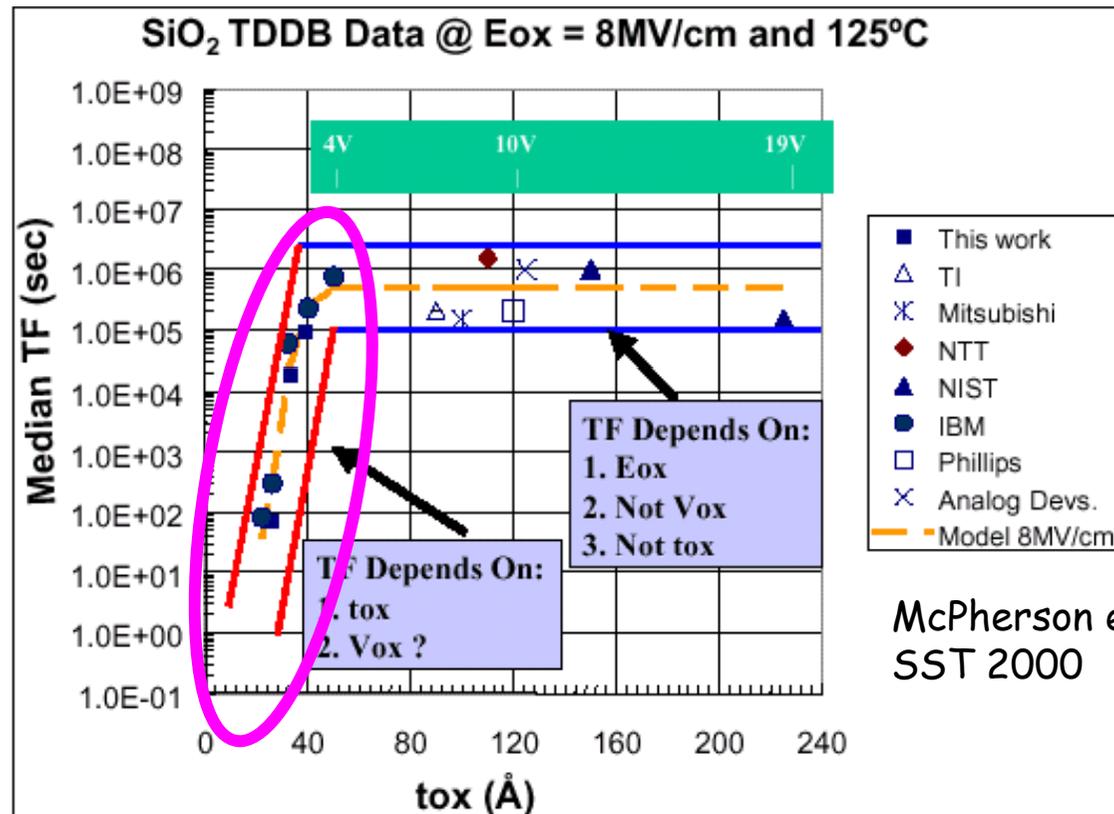
Below the physical thickness of 1.5nm the gate leakage current exceeds 1A/cm<sup>2</sup>

Thinner oxides  $\Rightarrow$  higher tunneling currents

**GROWING POWER CONSUMPTION**

# Time-to-breakdown vs. oxide thickness

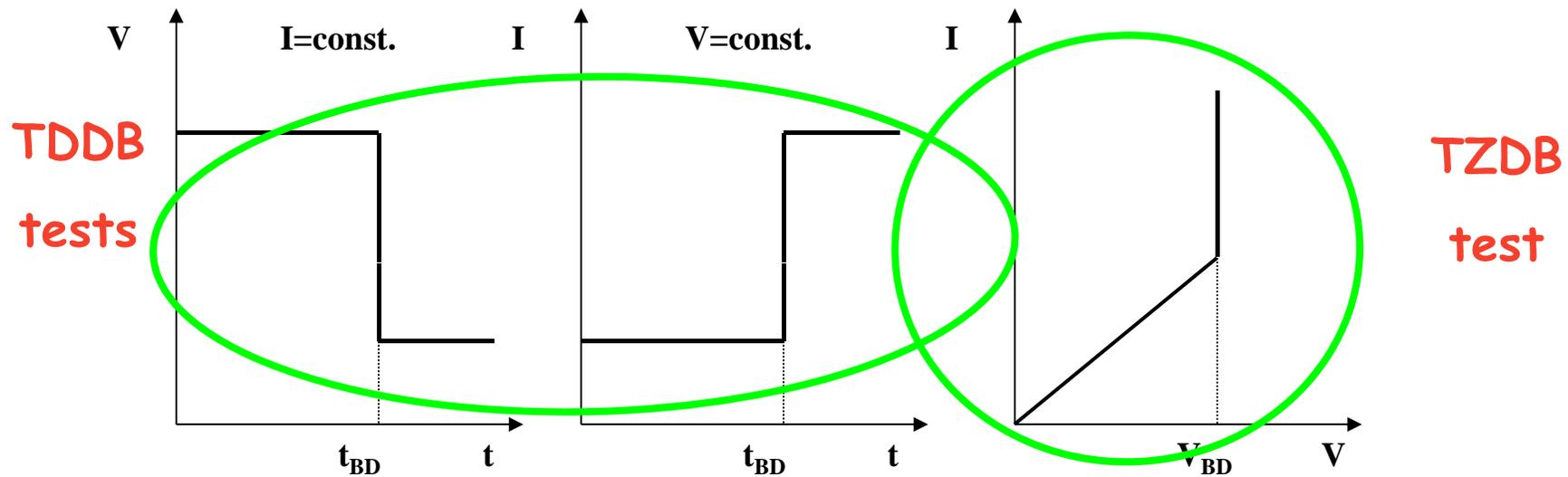
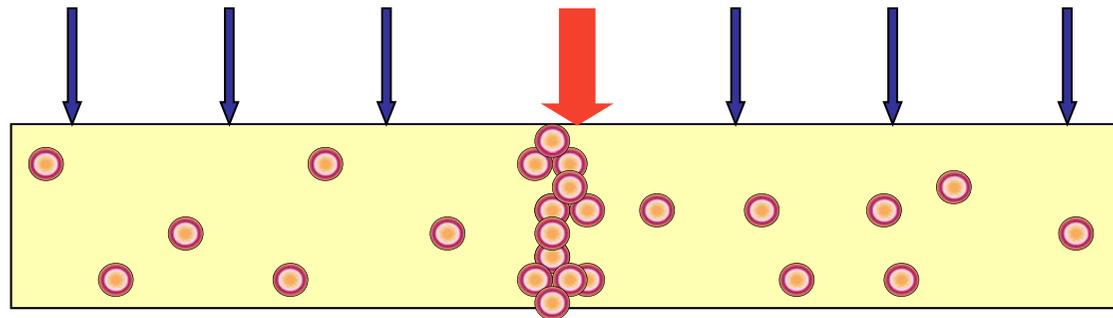
Thinner oxides  $\Rightarrow$  Reduction of the time-to-failure



**LESS RELIABLE DEVICES**

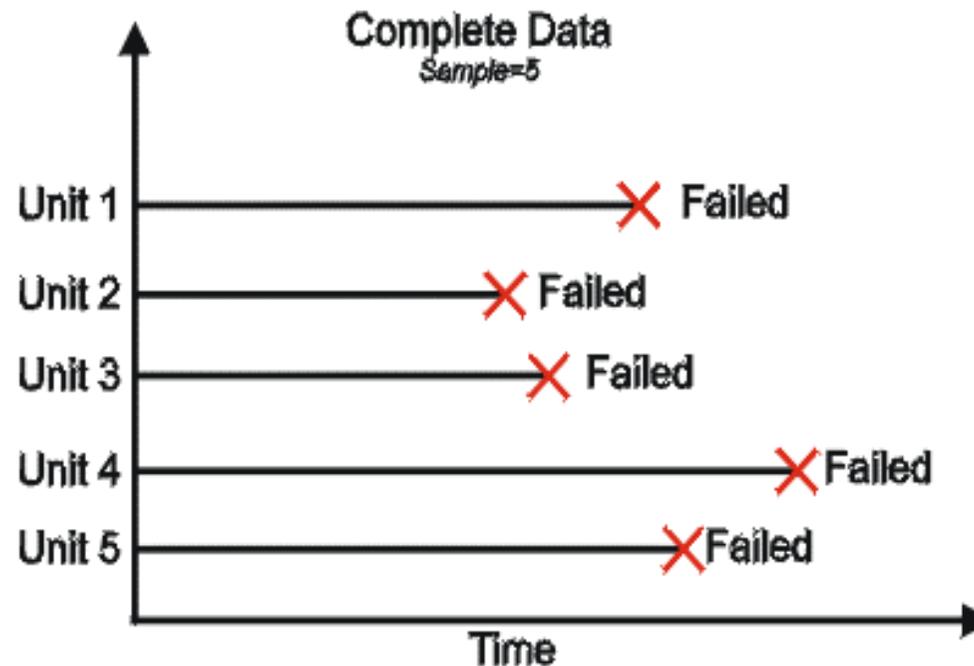
# What is a breakdown event?

Local lost of the insulating capability as a result of the generation and accumulation of defects



# Evaluation of time or charge-to-breakdown

Samples are subjected to identical stress conditions



Theoretical population models are required to characterize lifetimes

# The Weibull distribution



$$F(t) = 1 - e^{-(t/c)^\beta}$$

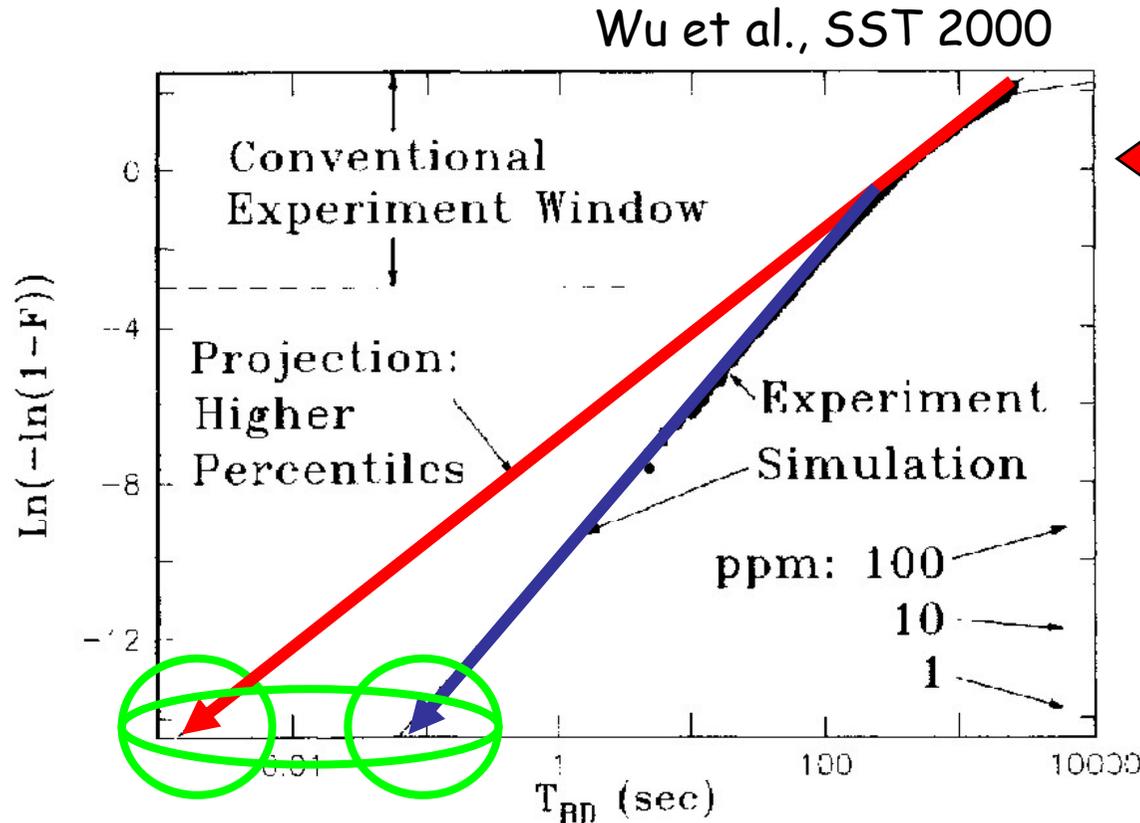
$c$ : characteristic life or scale parameter  
 $\beta$ : Weibull slope or shape parameter

"Weibit"

$$\ln[1 - F(t)] = -(t/c)^\beta$$
$$\ln\{-\ln[1 - F(t)]\} = \beta \ln t - \beta \ln c$$
$$Y = \beta X + b$$

Weibull data are fitted by a straight line with slope  $\beta$

# The importance of knowing $\beta$



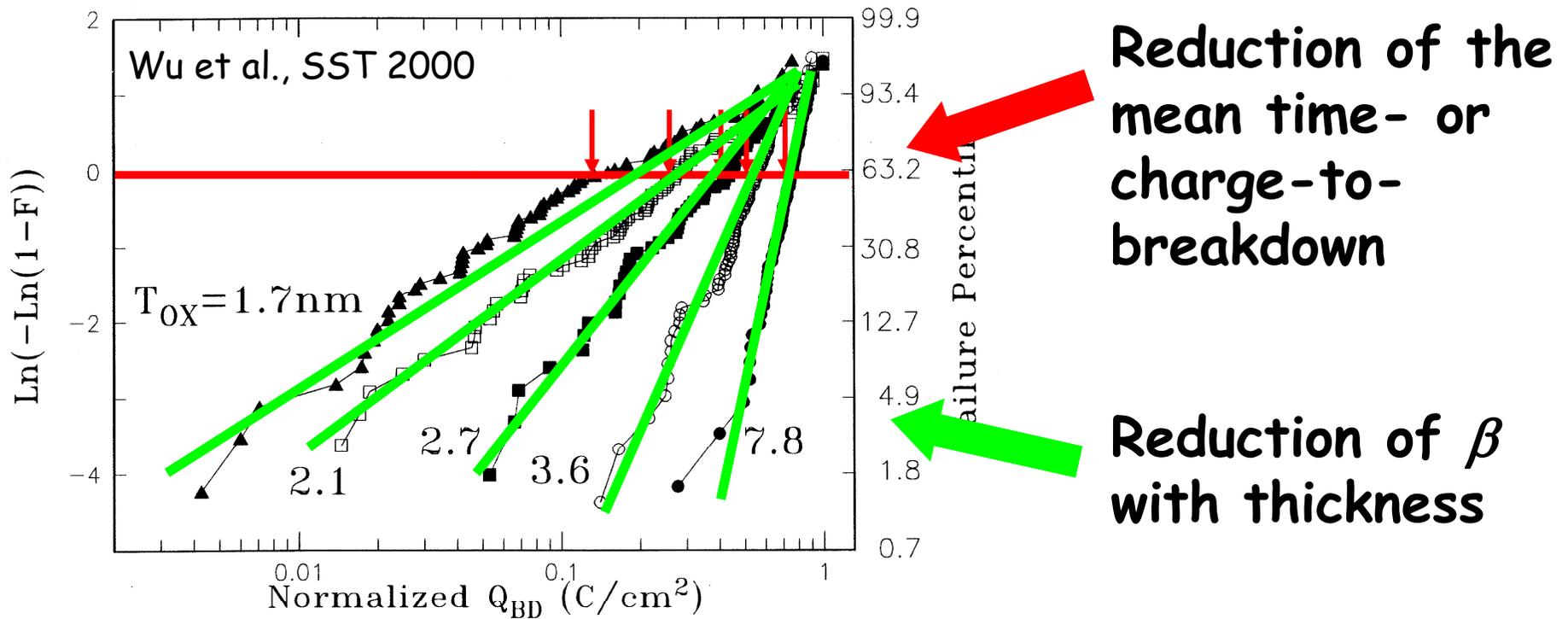
Caution should be exercised when projecting failure data

Recall that product failure rate must be specified at the low percentiles (parts per million)

Bad extrapolations underestimate or overestimate lifetimes

**GOOD UNDERSTANDING OF  $\beta$  IS STRONGLY REQUIRED**

# Thickness scaling of BD data



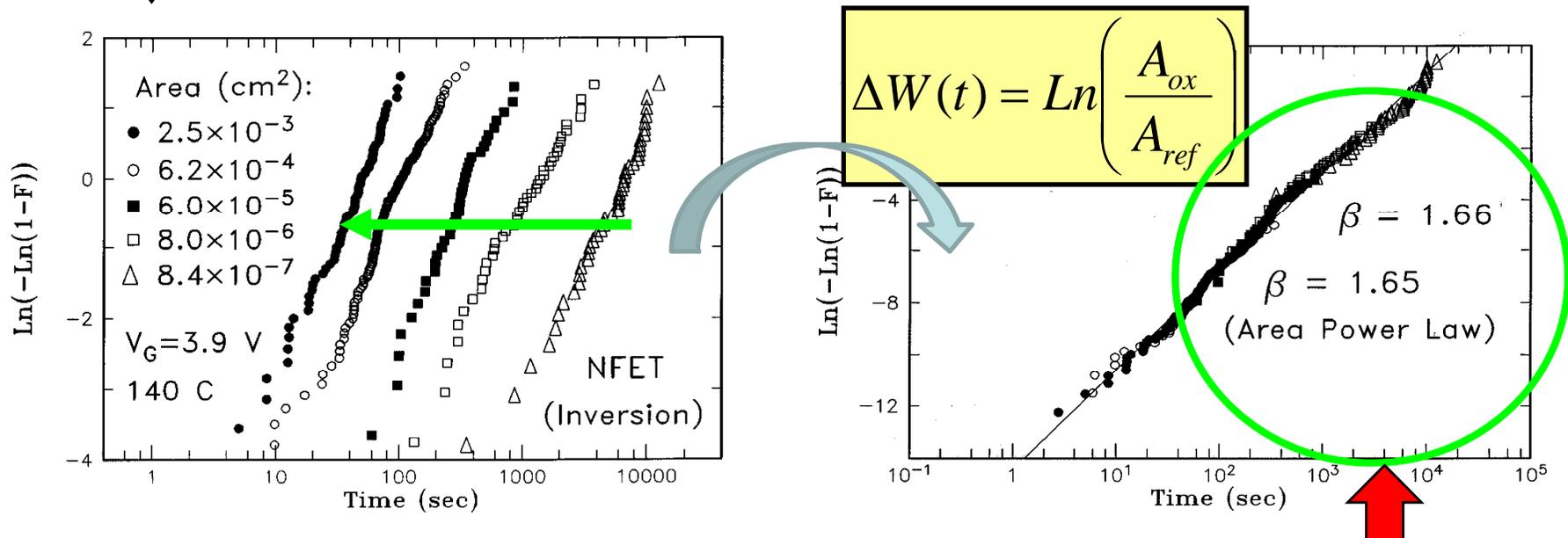
## PERCOLATION THEORY

the shallower distributions for thinner oxides are due to:

- decrease of critical defect density
- increase of statistical spread to form a conducting path

# BD statistics and area scaling

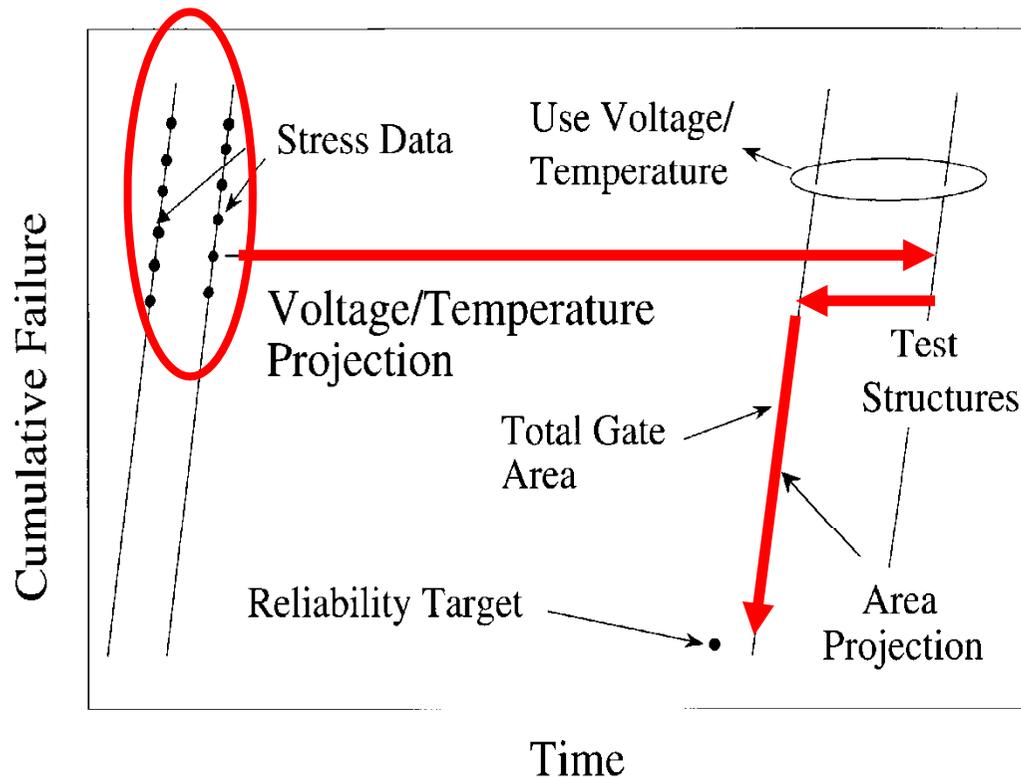

**Larger areas exhibit lower time-to-breakdown with same  $\beta$**



All curves can be merged into a single one by a vertical shift

**Breakdowns are randomly distributed over the device area which is indicative of a Poisson process**

# The task of a reliability engineer



Data are obtained under accelerated stress in test structures

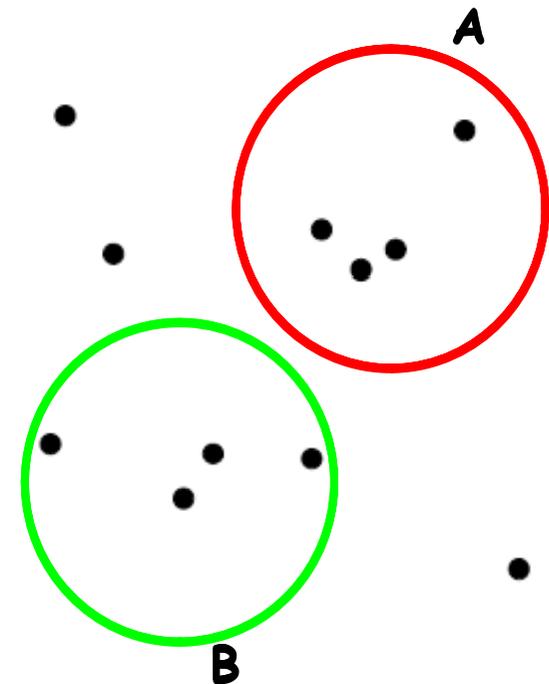
Assuming Poisson statistics

- Extrapolation to operating conditions (voltage and temperature)
- Extrapolation to total gate area (circuit level)
- Extrapolation to low percentiles (parts per million)

# 2D Poisson process

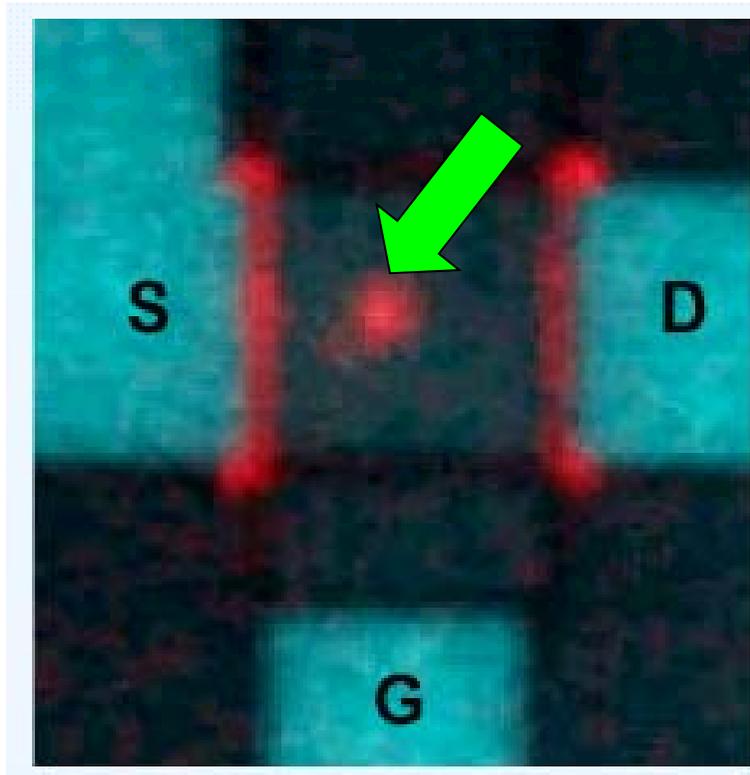
- Basic 'reference' or 'null model' model of a point process in the plane, also called Complete Spatial Randomness (CSR)

- The number of points falling in any region  $A$  has a Poisson distribution
- Given that there are  $n$  points inside region  $A$ , the locations of these points are uniformly distributed inside  $A$
- The contents of two disjoint regions  $A$  and  $B$  are independent

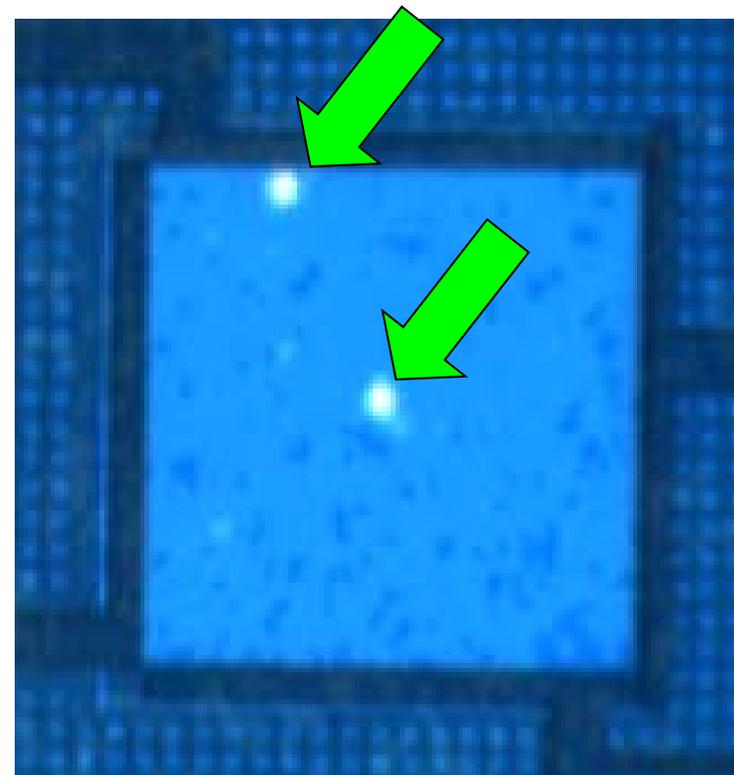


**One BD event in many small devices is equivalent to many BD events in a single large area device**

# Visualization by light emission microscopy



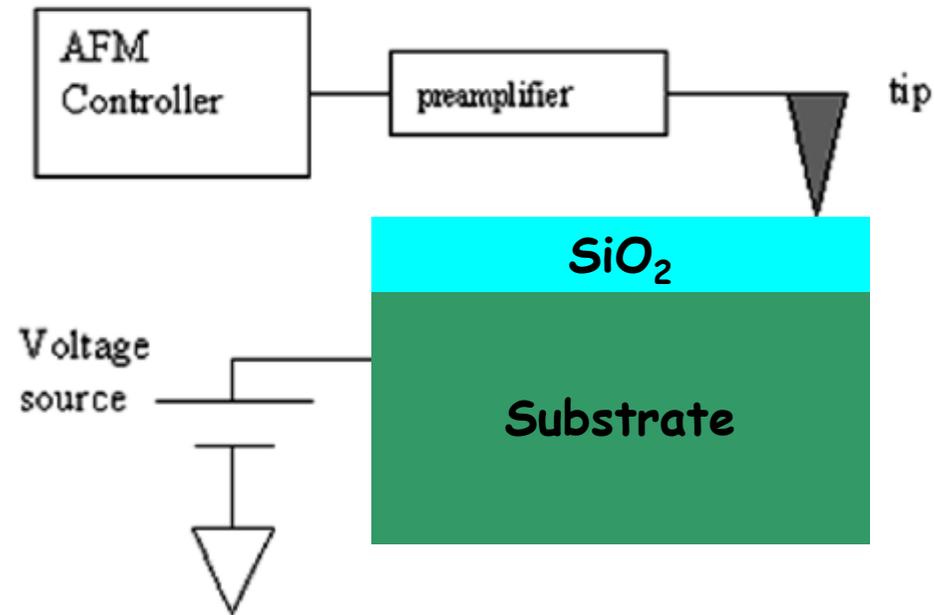
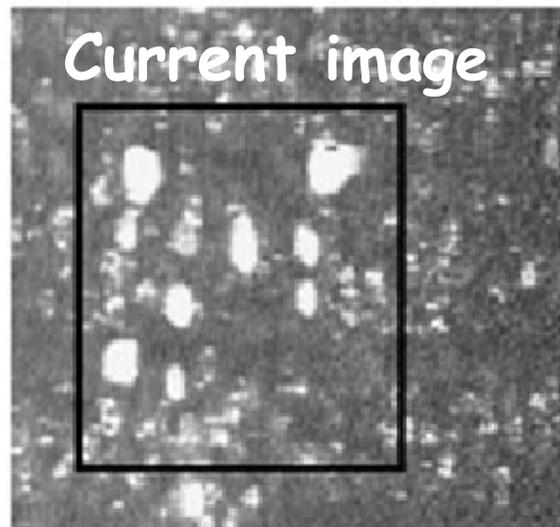
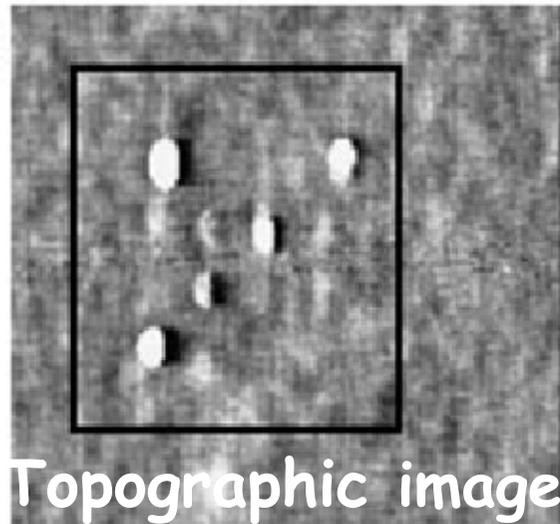
IMEC (2001)



Bruyère *et al*, IRPS 2000

**One or several BD spots can be detected  
in a single device**

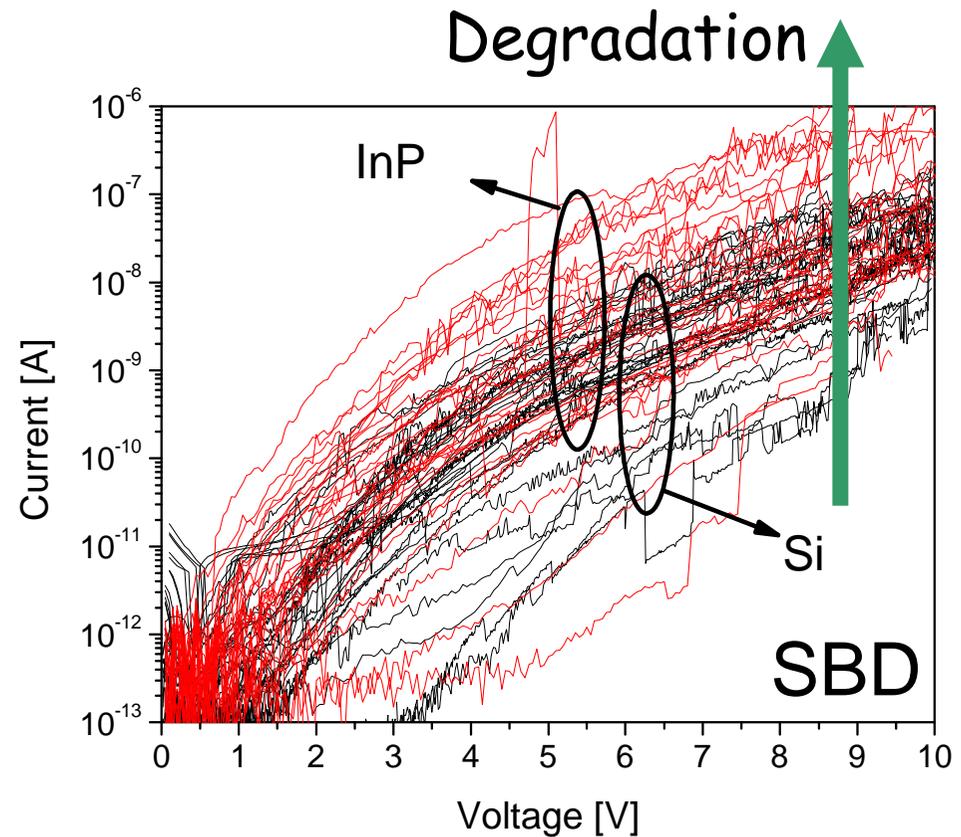
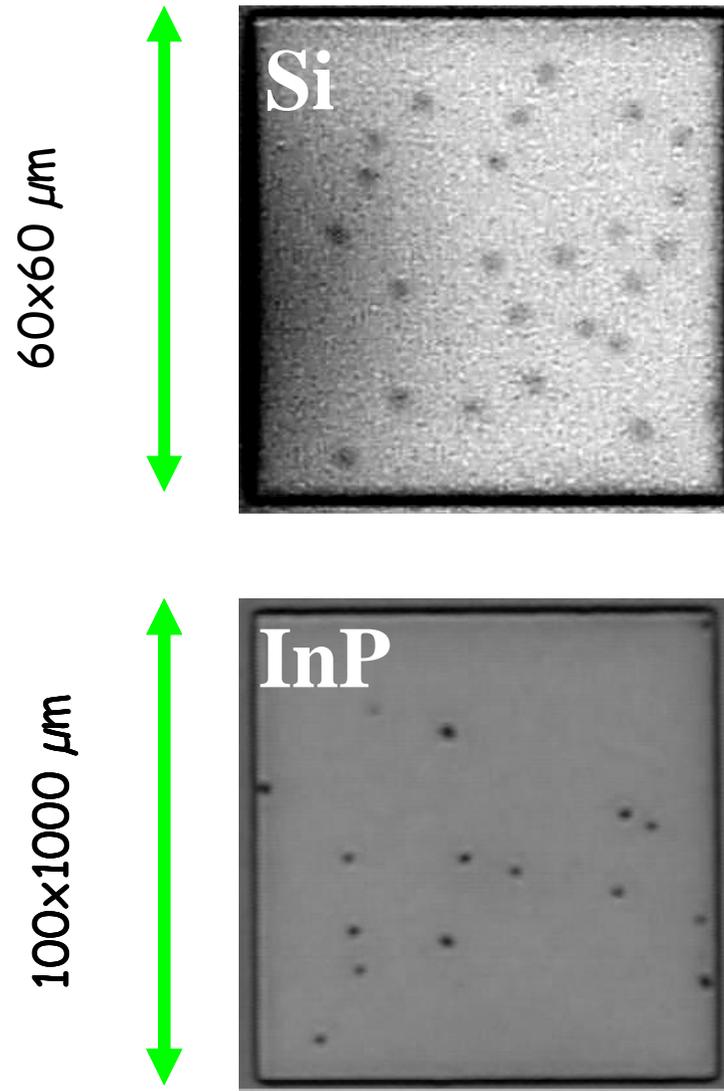
# Imaging BD spots with a Conductive-AFM



The conductive tip plays the role of the metal electrode of a MOS capacitor

Porti *et al*, TDMR 2002

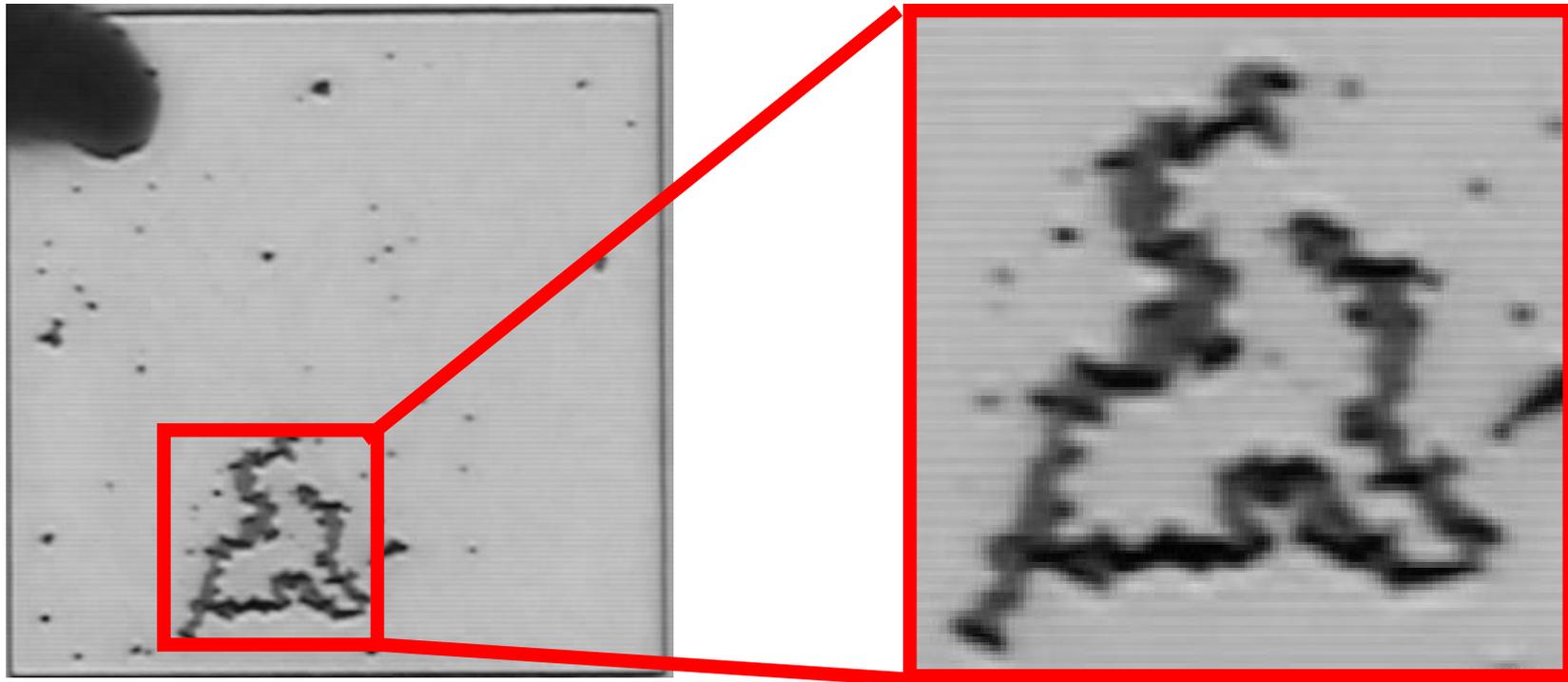
# Direct visualization in MOS capacitors



I-V characteristics after successive voltage sweeps

# Direct visualization in MOS capacitors

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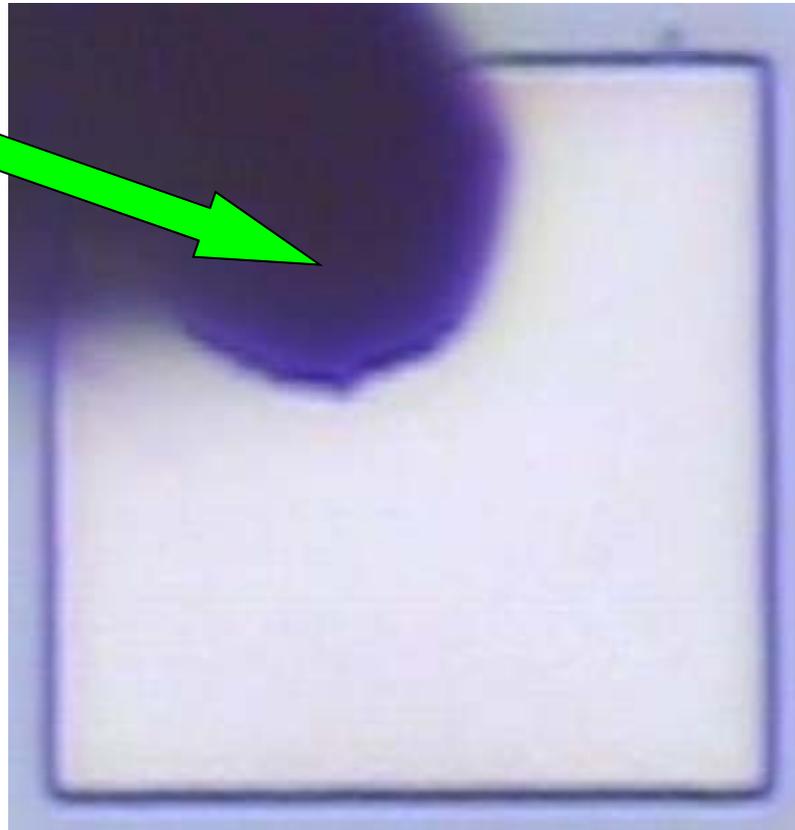


Lateral propagation of damage in the form of random walks

# Multiple BD spots generation

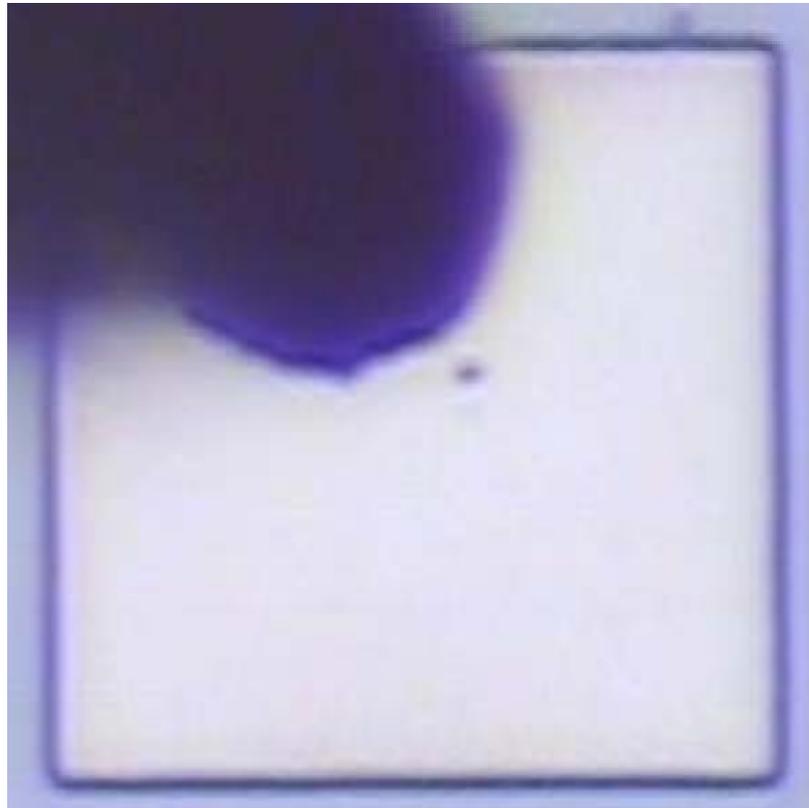
NiSi/MgO/InP (metal gate/High-K/III-V structure)

Voltage probe  
needle



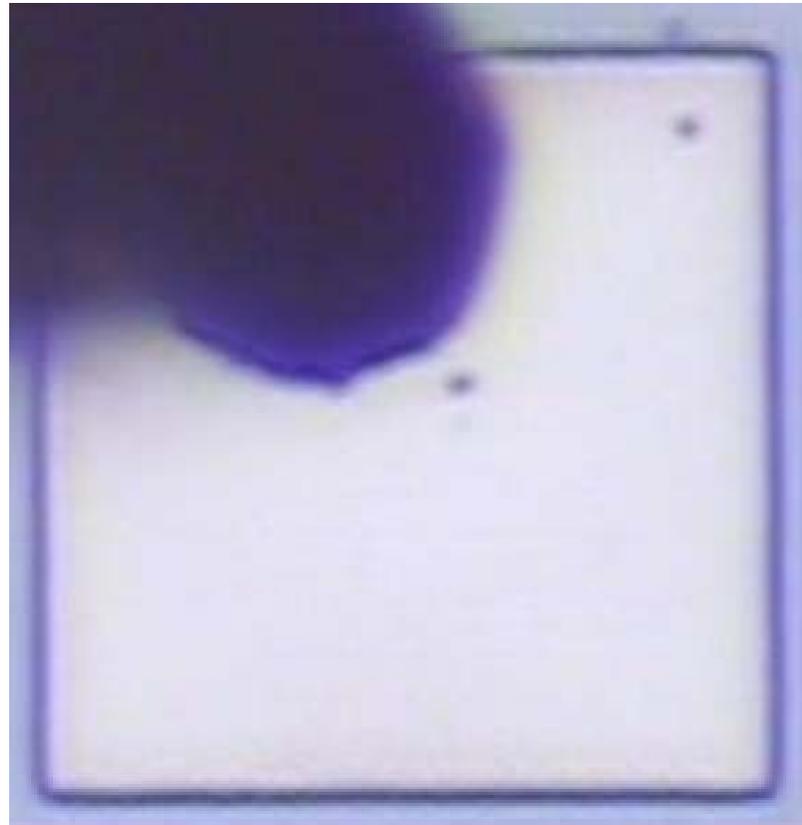
# Multiple BD spots generation

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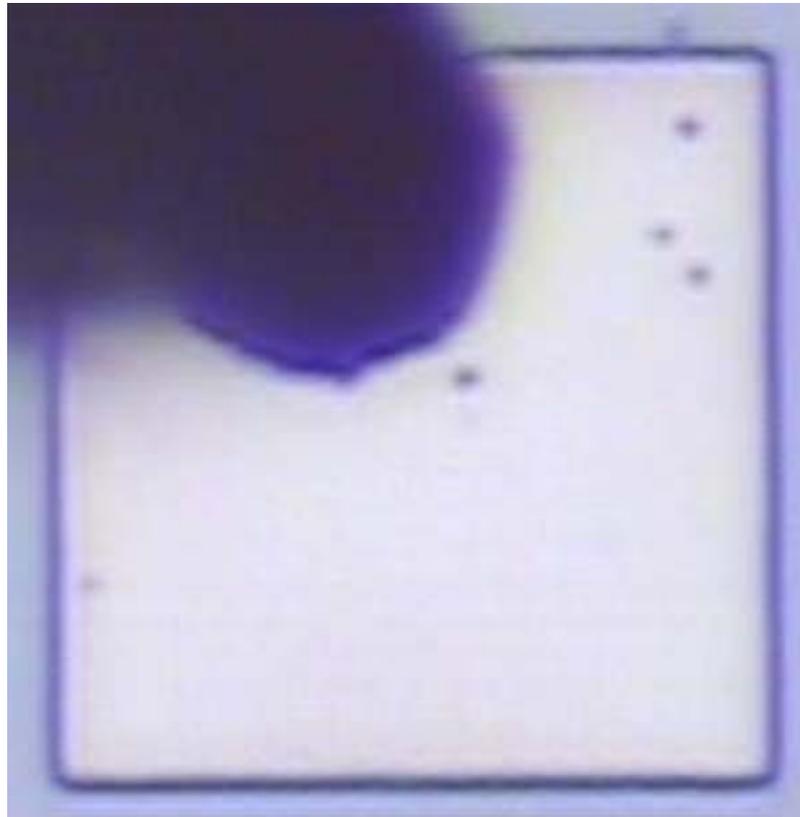
# Multiple BD spots generation

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# Multiple BD spots generation

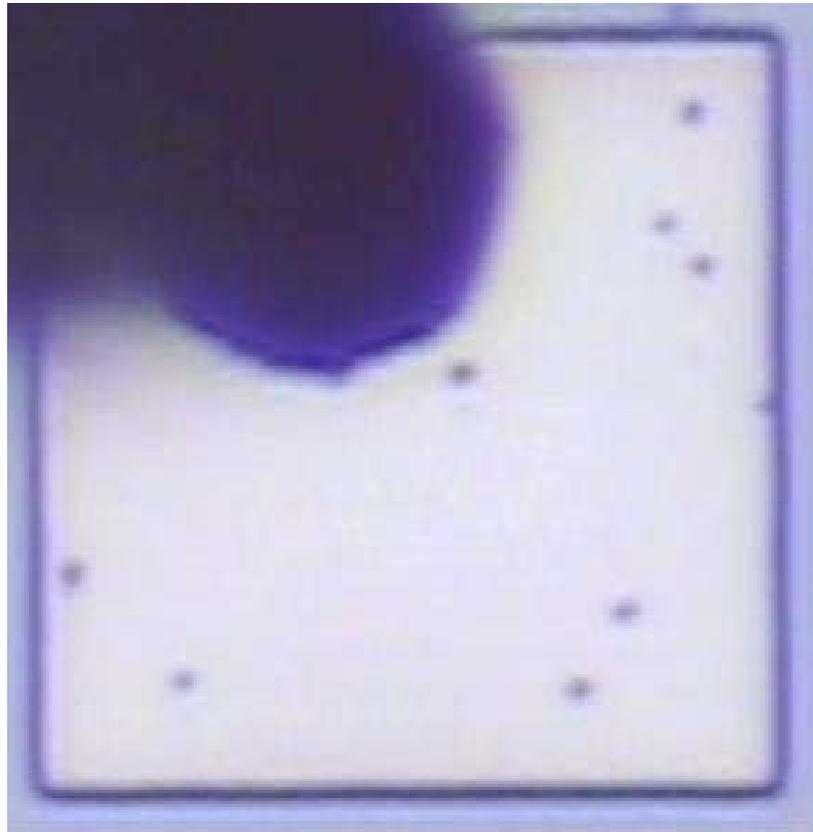
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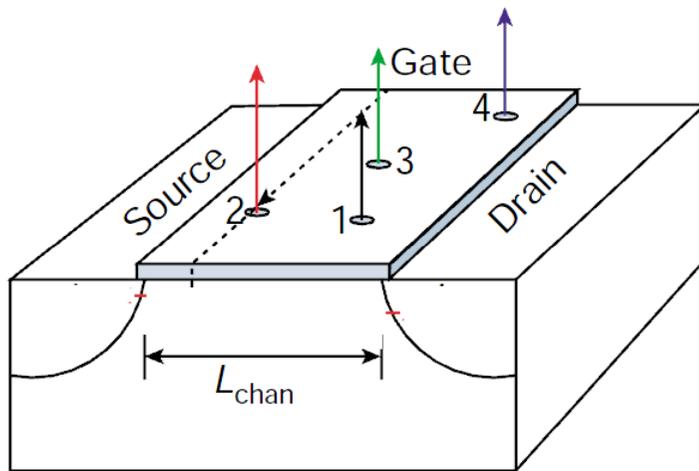
# Multiple BD spots generation

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Is the BD spot distribution compatible with a Poisson process?



Is there any interaction among them?

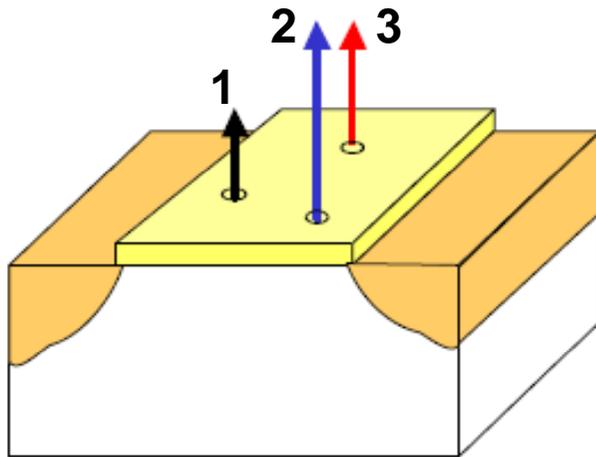


- ICs may continue to operate immediately after a BD event
- “if the localized current through the first spot forces a subsequent BD to occur in close proximity then the transistor could rapidly become inoperative”

M. Alam, IRPS'03

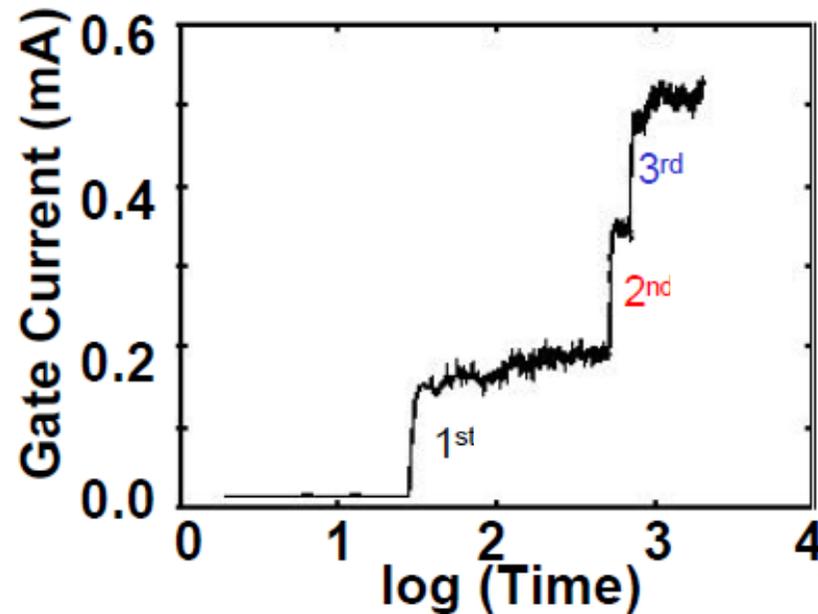
**Therefore, it is critically important to precisely establish the degree of correlation among the positions and times of breakdown events**

# Temporal correlation



Does the time to  
n-breakdown  
depend on the time  
to n-1 breakdown?

Each step in the  
current evolution is  
associated with the  
creation of a BD spot



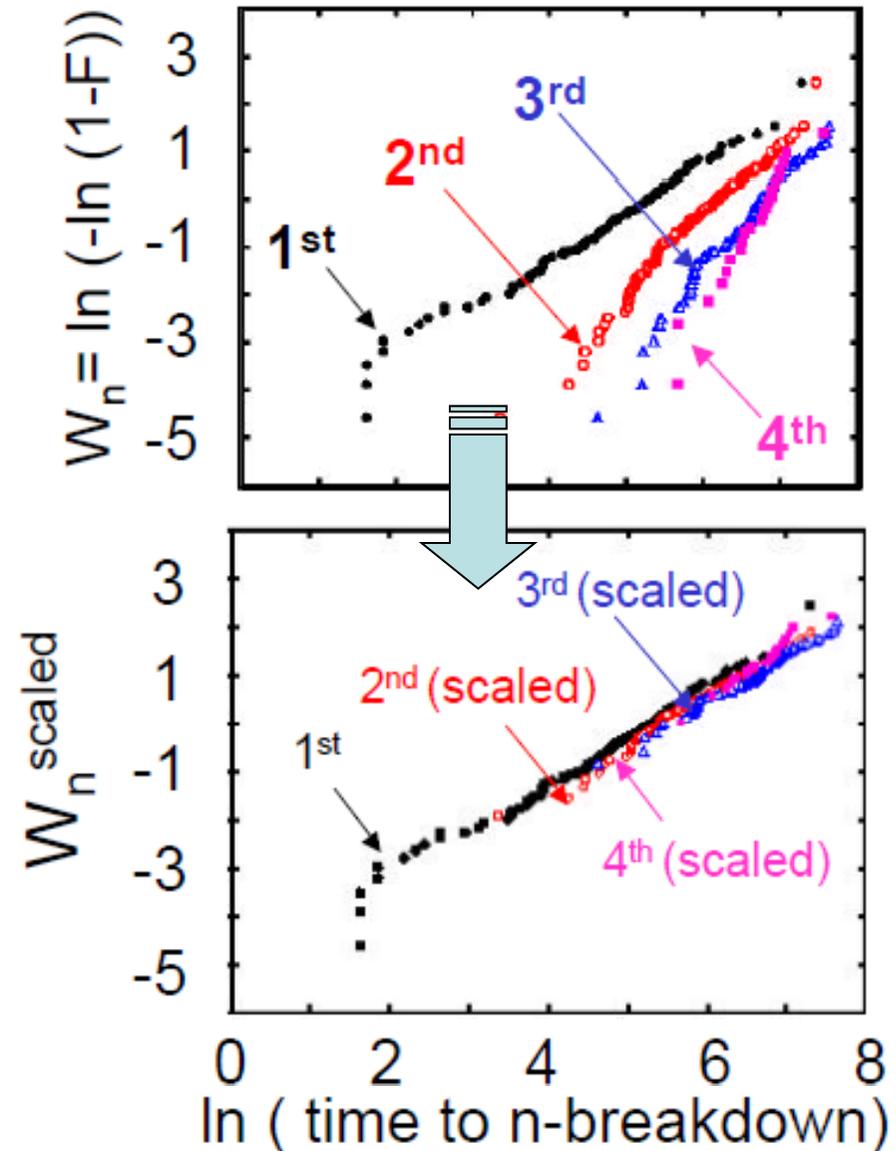
# Weibits for successive BD events



Distribution of the time to  
n-breakdown as measured  
(order statistics)

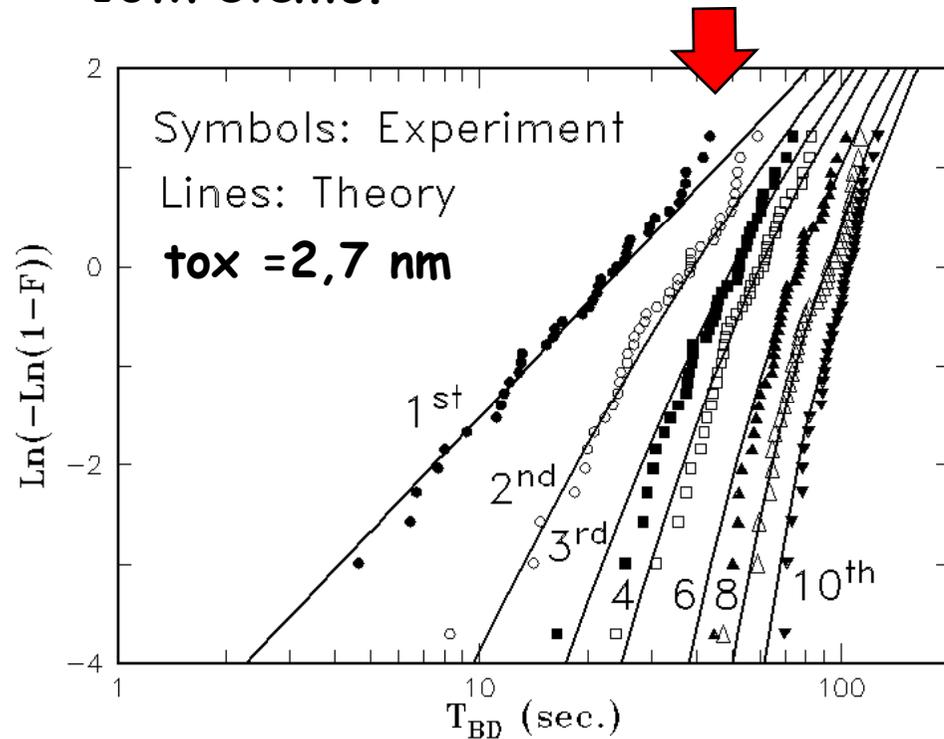
Transformed data  
assuming temporal  
uncorrelation

**The BD spots do  
not exhibit temporal  
correlation**



# Modeling of BD order statistics

Successive BD distributions for the 1st, 2nd, 3rd, 4th, 6th, 8th, and 10th events.



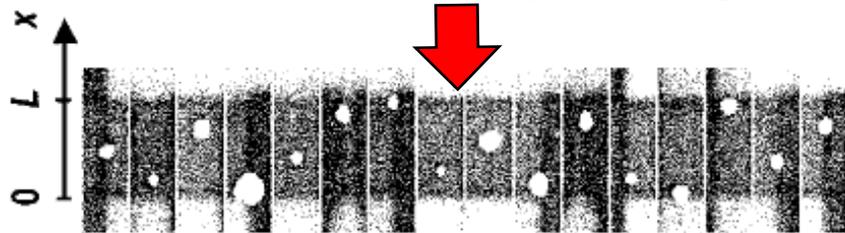
- These are not straight lines in the Weibull plot
- Order statistics can be modeled assuming that the generation of successive BD paths is uncorrelated and uniform across the oxide area

**Again, it is concluded that the BD spots are temporally and spatially uncorrelated**

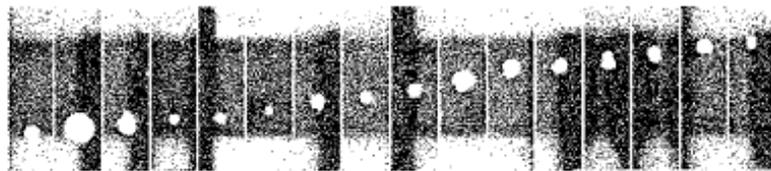
Suñé *et al*, EDL 2003

# Localization of a single BD spot

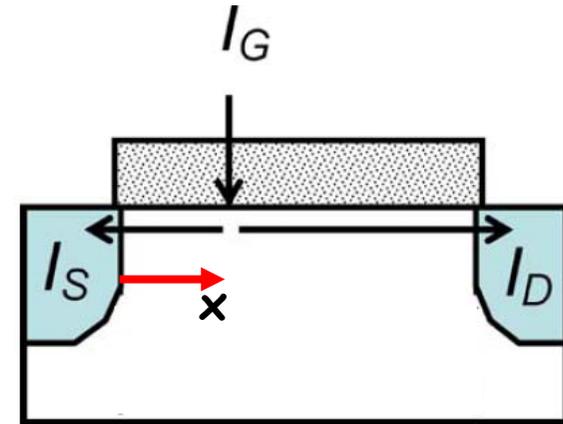
Emission microscope images of 16 nFETs



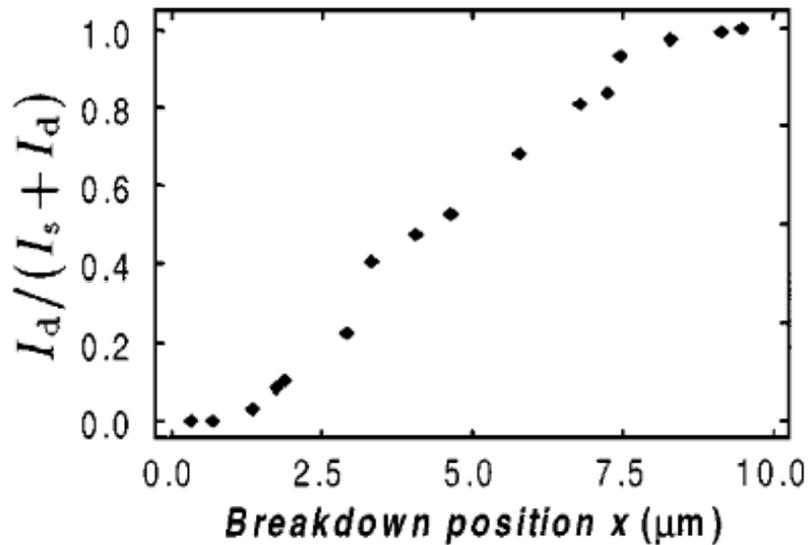
Unsorted



Sorted



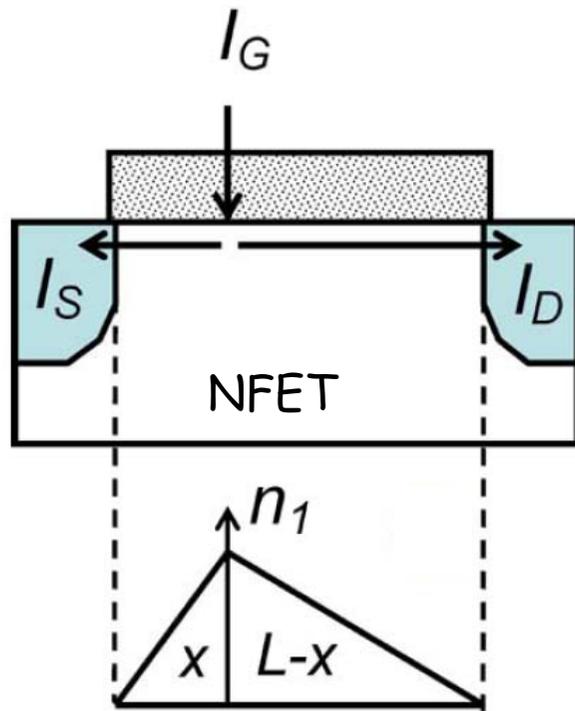
$$\frac{x}{L} = \frac{I_{Drain}}{I_{Drain} + I_{Source}}$$



Approximately uniform distribution of the breakdown spots along the gate length

Degraeve *et al*, TDMR 2001

# 1D theory for the current-ratio method



From the drift-diffusion equation in accumulation:

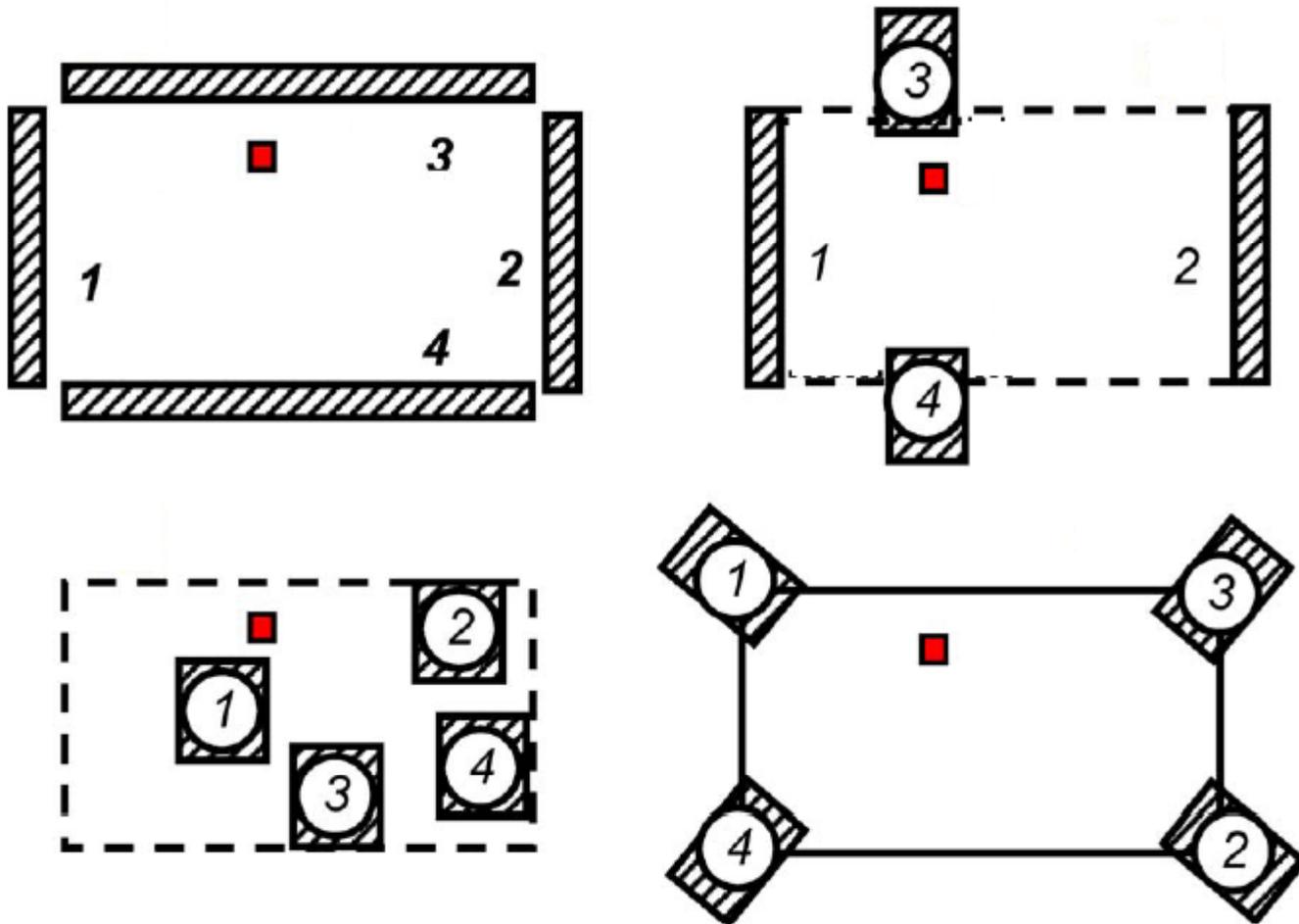
~~$$J = qn\mu_n \nabla \phi + qD_n \nabla n$$~~

- $n$ : electron density
- $\mu_n$ : electron mobility
- $D_n$ : electron diffusion constant
- $\Phi$ : channel potential

and using the continuity equation  $\nabla \cdot J = 0$

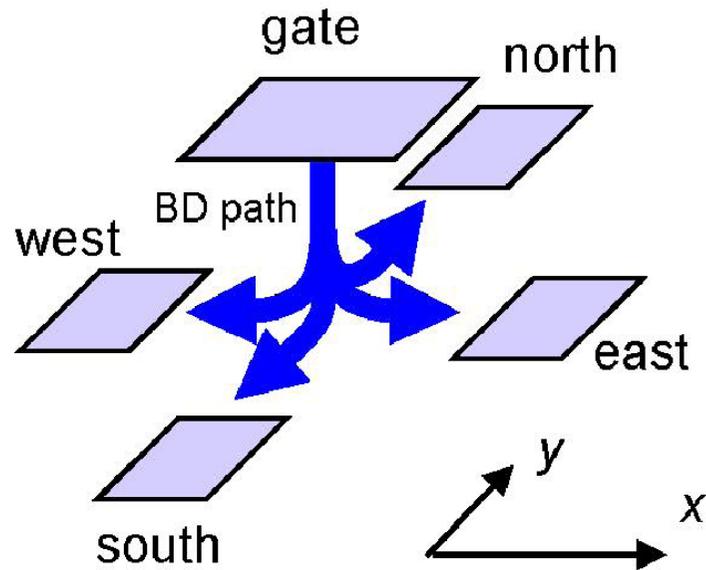
$$D_n \nabla^2 n = 0 \begin{cases} \rightarrow I_S = qAD_n n_1 / x \\ \rightarrow I_D = qAD_n n_1 / (L - x) \end{cases} \rightarrow \boxed{\frac{x}{L} = \frac{I_D}{I_D + I_S}}$$

## Five probe van der Pauw technique (5P-VDP)



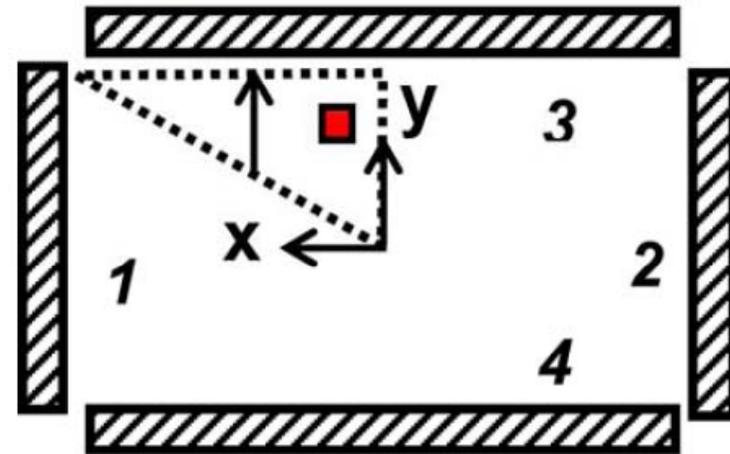
Four different testers to locate the  $(x,y)$  positions of a BD spot

# Localization in 2D

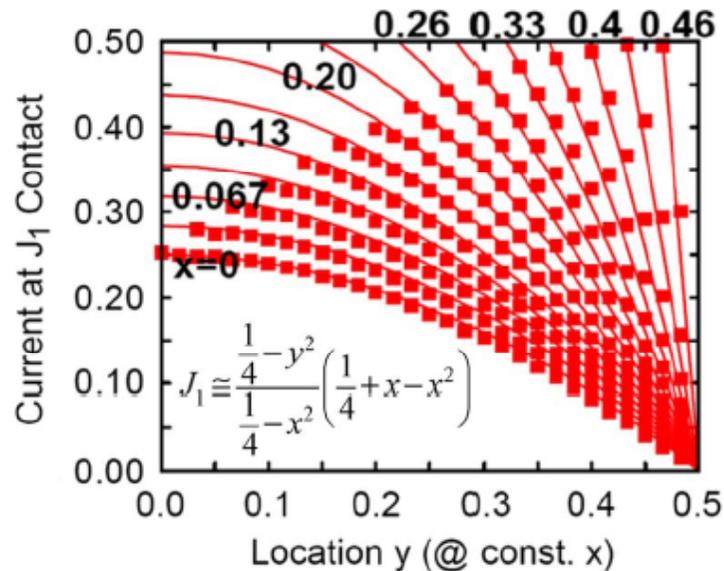


- The electrons injected through the BD spot are collected by the four grounded contacts
- The ratios of the currents depend on the relative distances of the BD spots from the respective contacts

The ordering  $J_{\max} > J_1 > J_2 > J_{\min}$  allows locating the “triangle” within which the BD must have occurred



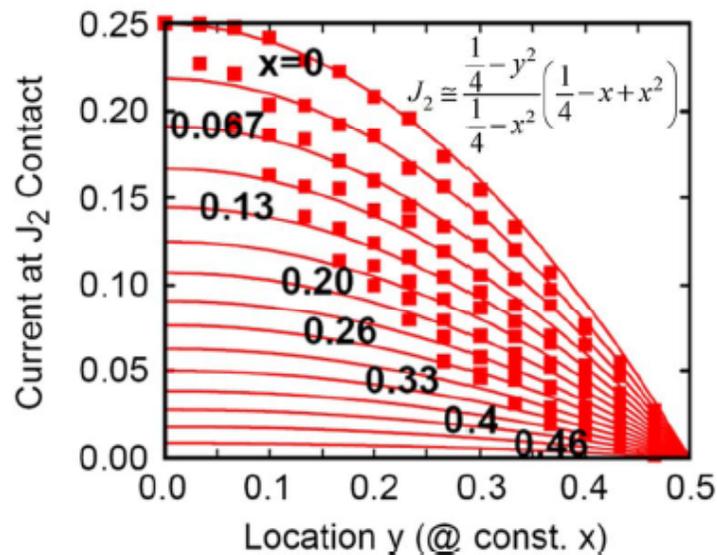
# Localization in 2D



Using symmetry arguments

$$J_1 \approx \left( \frac{0.25 - y^2}{0.25 - x^2} \right) (0.25 + x - x^2)$$

$$J_2 \approx \left( \frac{0.25 - y^2}{0.25 - x^2} \right) (0.25 - x + x^2)$$

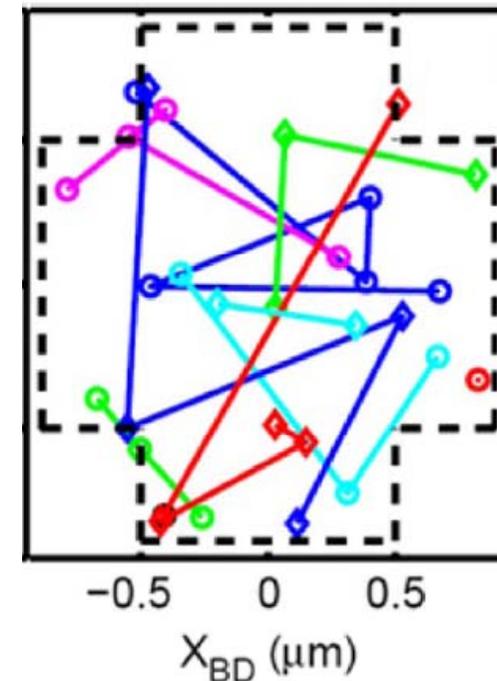
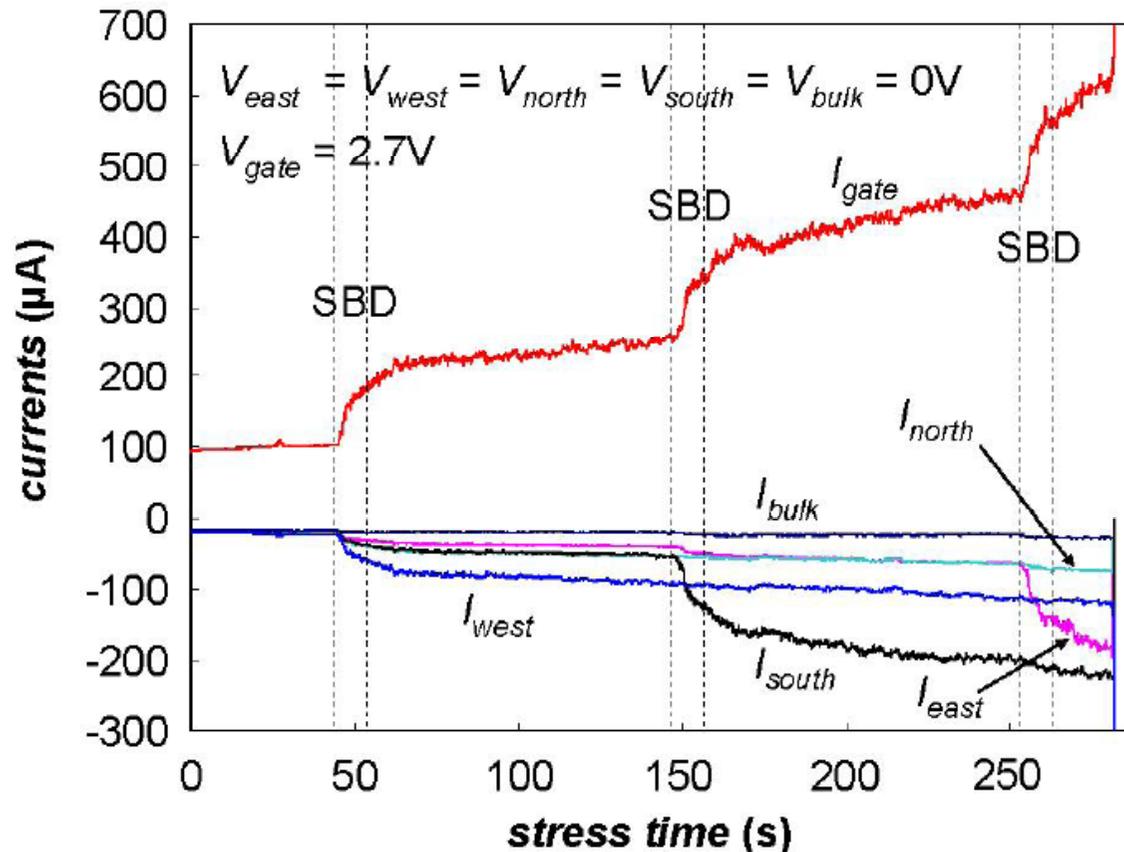


We can determine the position  $(x,y)$  from

$$x = 0.5 - \sqrt{\frac{0.5J_2}{J_1 + J_2}}$$

$$y = \sqrt{0.25 - 2(J_1 + J_2)(0.25 - x^2)}$$

# Localization in 2D

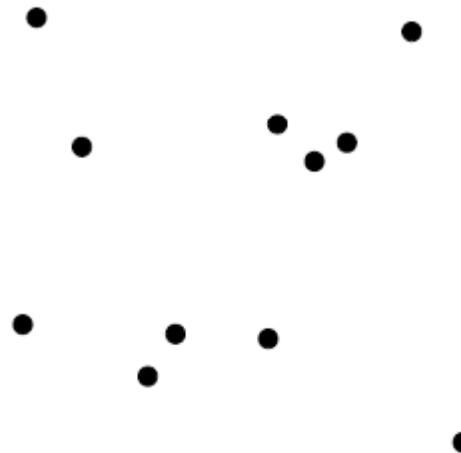


Current traces recorded during a constant voltage stress allow detecting the BD spots locations

# Spatial statistics



A spatial point process is a random pattern of points in  $d$ -dimensional space (usually  $d=2$  or  $d=3$ ): trees in a forest, bird nests, disease cases, the locations of point-like defects in a silicon crystal wafer or ... **breakdown spots**

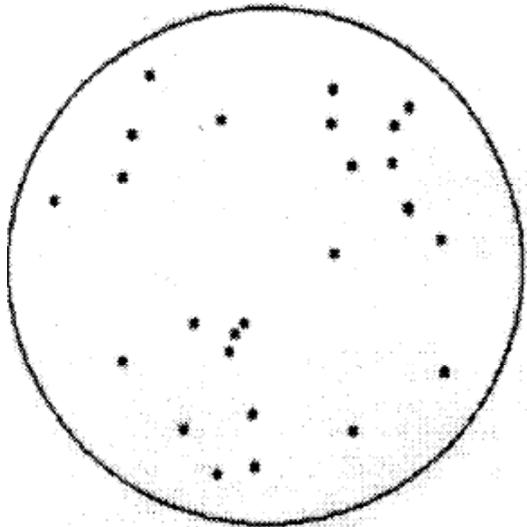


The objective is to assess whether they interact or not, i.e. if they are spatially correlated

# Visual defect metrology



Wafer defect map (particles, opens, shorts, film thickness variations, discolorations etc.)



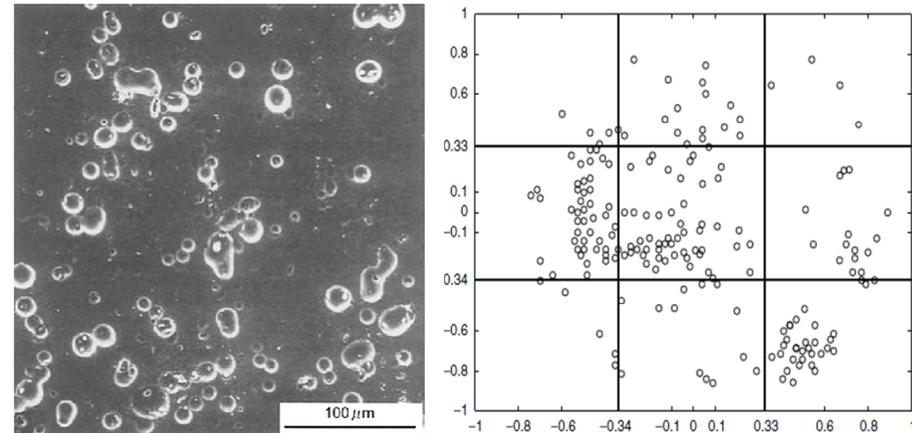
Cunningham *et al*,  
TSM (1998)

Infrared light emission at  
breakdown sites in MIS  
tunnel diodes



Mihaychuk *et al*, JAP (2005)

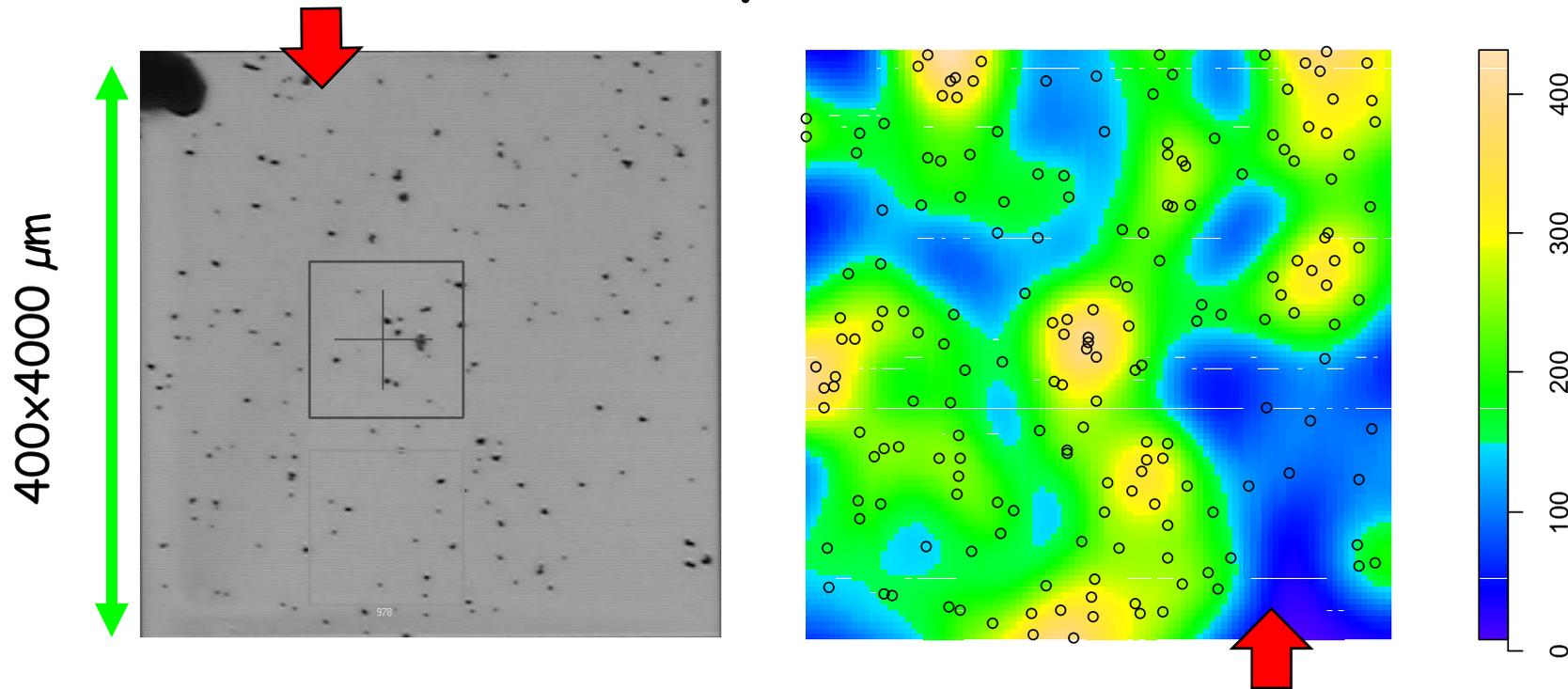
## Corrosion patterning



Lopez de la Cruz *et al*, CS (2008)

# Point pattern analysis techniques

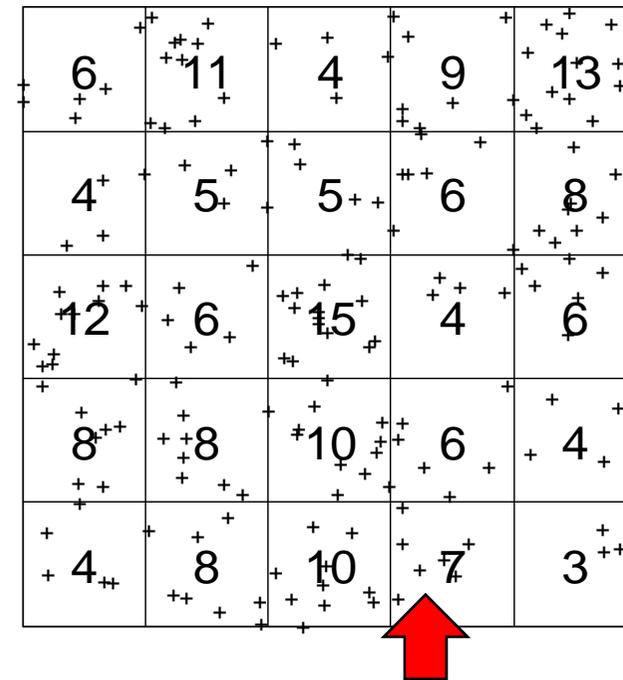
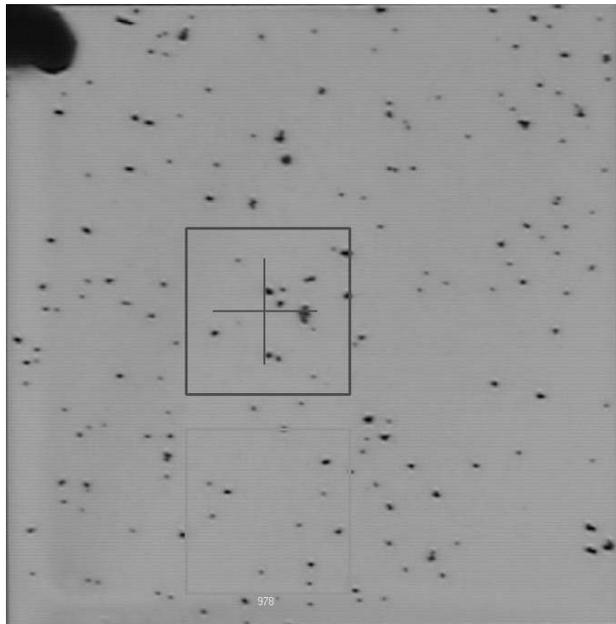
For this realisation 182 points were found



The **intensity plot** reveals that the points are not uniformly spread but there are empty gaps and clusters of points. This is consistent with a 2D homogeneous Poisson process

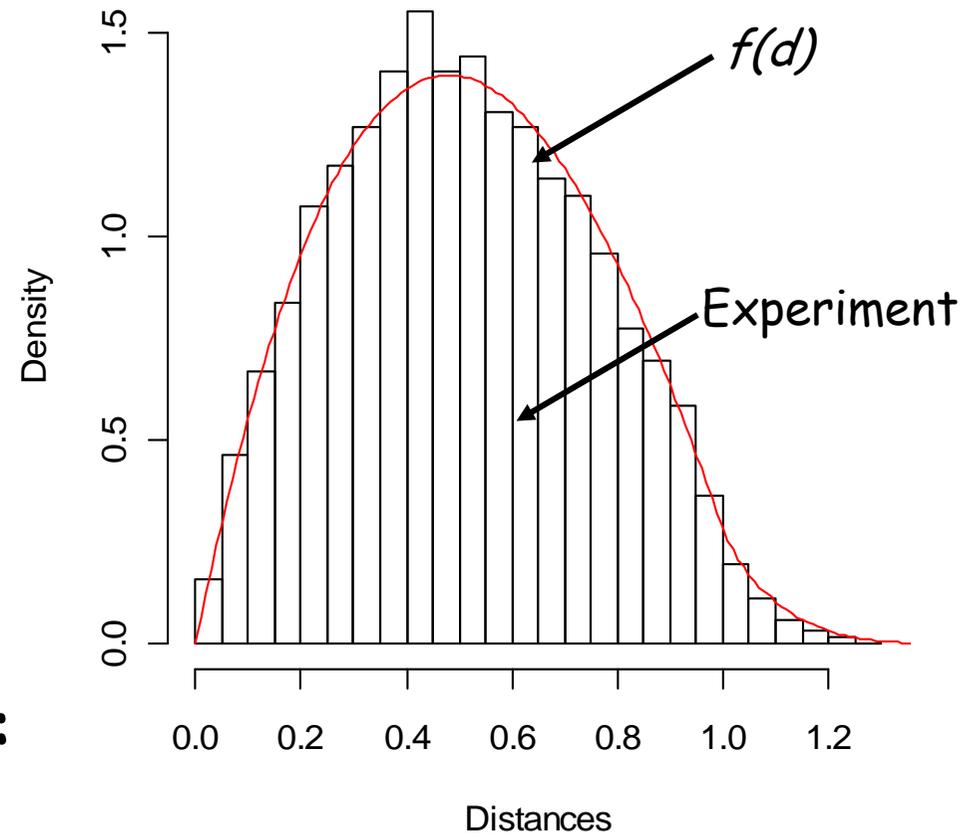
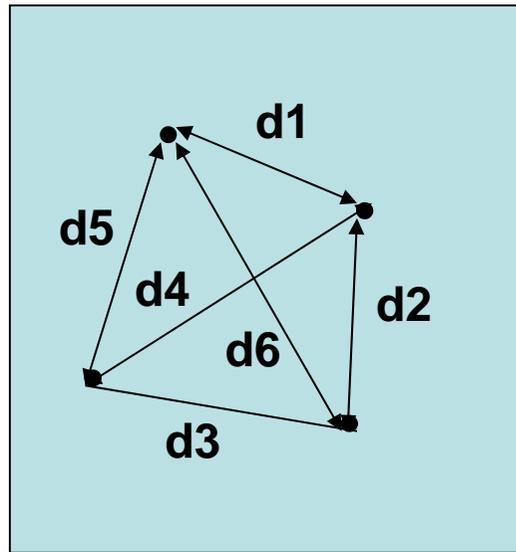
Miranda *et al*, IRPS 2010

# Analysis of the BD spots spatial distribution



**Quadrat count method:** the frequency distribution of the number of events in each cell is used to compute the variance-to-mean ratio. If  $VTMR=1$  the pattern is random

# Interpoint distances distribution

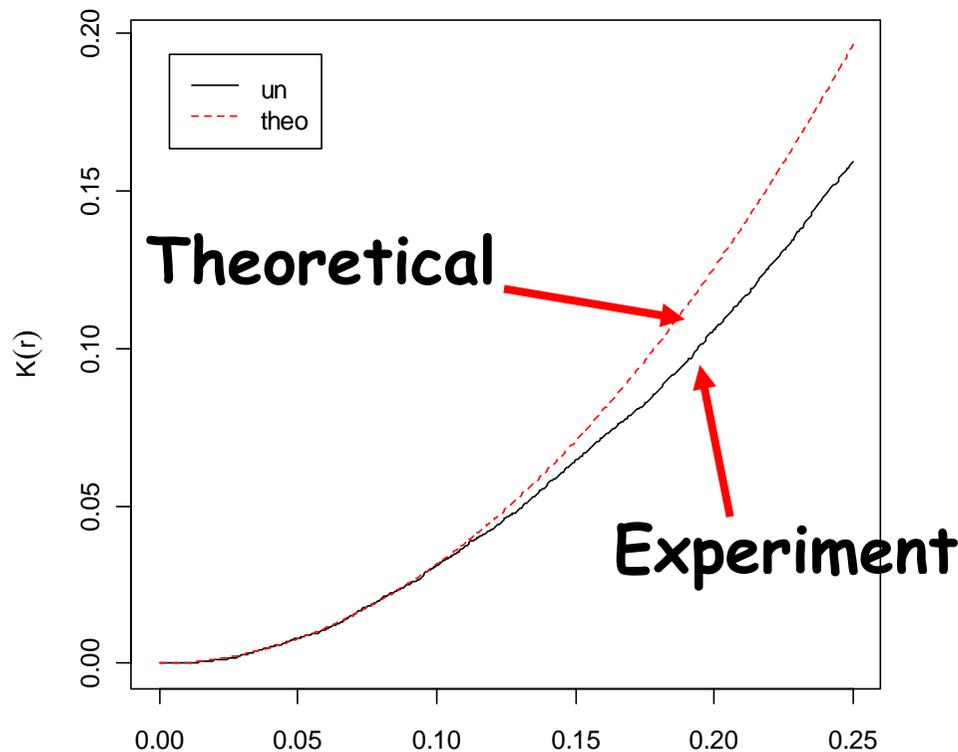


For random points in  $1 \times 1$  :

$$f(d) = \begin{cases} 4d \left[ \frac{\pi}{2} - 2d + \frac{d^2}{2} \right] & 0 \leq d \leq 1 \\ 4d \left[ \arcsin \left( \frac{1}{d} \right) - \arccos \left( \frac{1}{d} \right) - 1 - \frac{d^2}{2} + 2\sqrt{d^2 - 1} \right] & 1 < d \leq \sqrt{2} \end{cases}$$

# Functional summary estimator K

**K(r)** or **Ripley's function** is related to the expected number of other points of the process within a distance  $r$  of a typical point of the process



For a Poisson process, the number of points in a circle increases as the area of the circle:

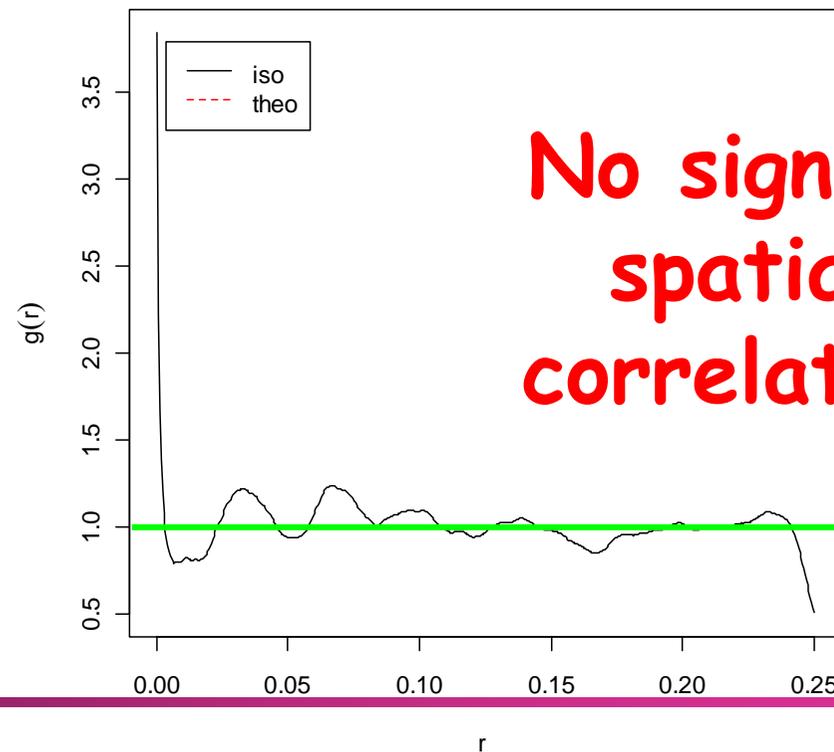
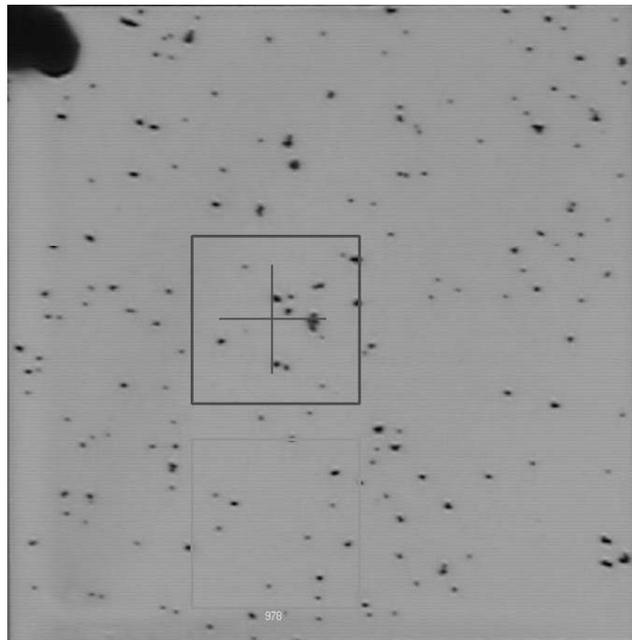
$$K_{CSR}(r) = \pi r^2$$

Miranda *et al*, Mic Rel 2010

# Pair correlation function

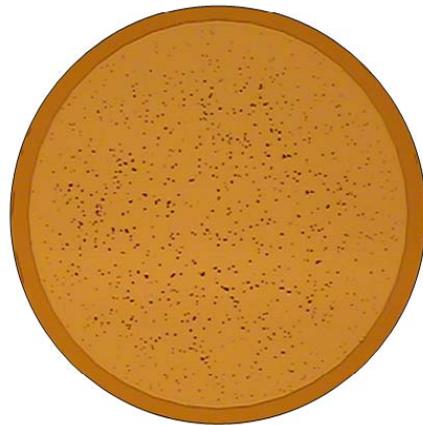


$$g(r) = \frac{1}{2\pi r} \frac{dK(r)}{dr} \left\{ \begin{array}{ll} = 1 & r \geq 0 \quad \text{Poisson process} \\ \geq 1 & \text{small } r \quad \text{cluster process} \\ \leq 1 & \text{small } r \quad \text{regular process} \\ = 0 & r \leq r_0 \quad \text{hard core potential} \end{array} \right.$$



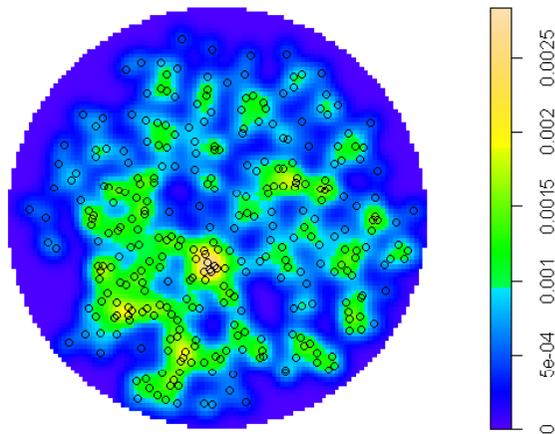
**No sign of  
spatial  
correlation**

# Failure events in circular MIM capacitors\*

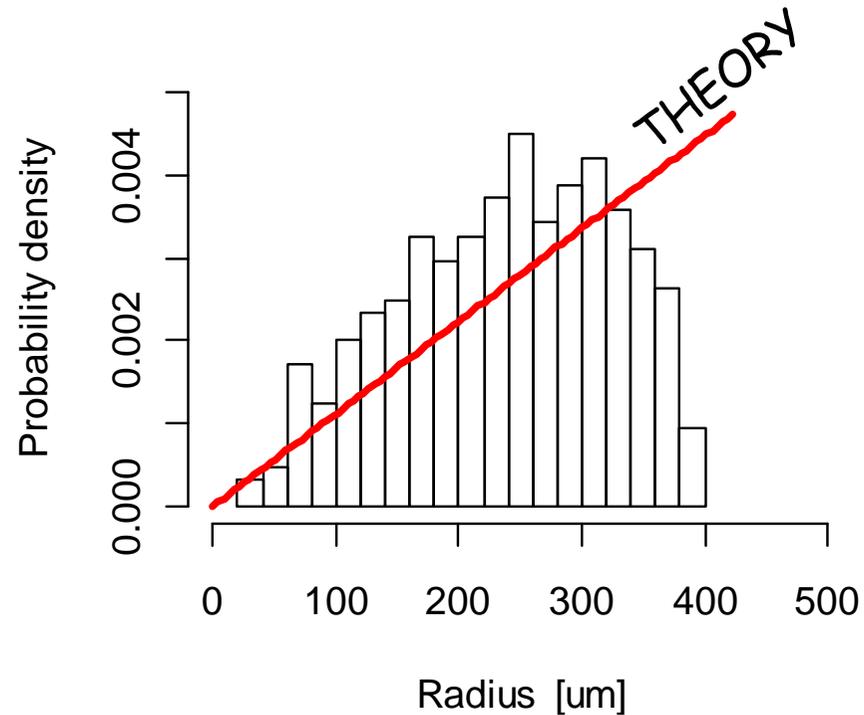


Pt/HfO<sub>2</sub>/Pt

Should we always expect CSR in MOS/MIM devices?

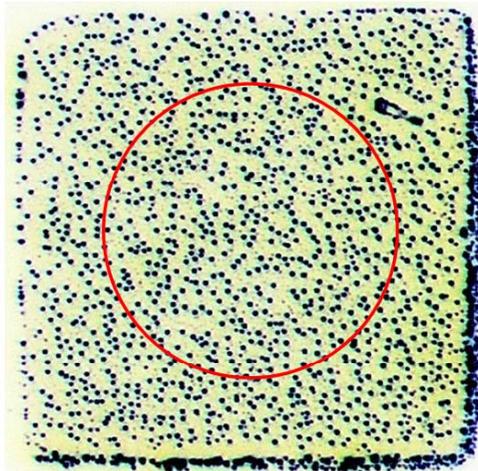


Low intensity at the edges



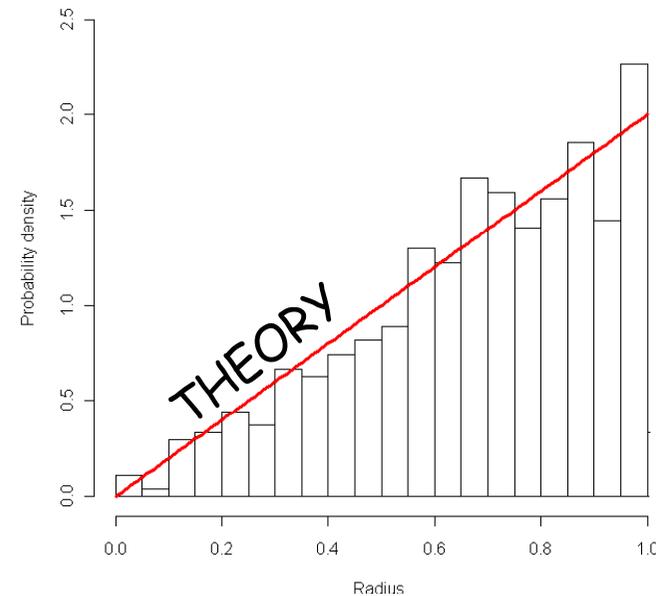
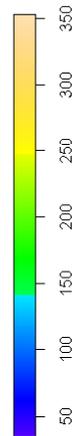
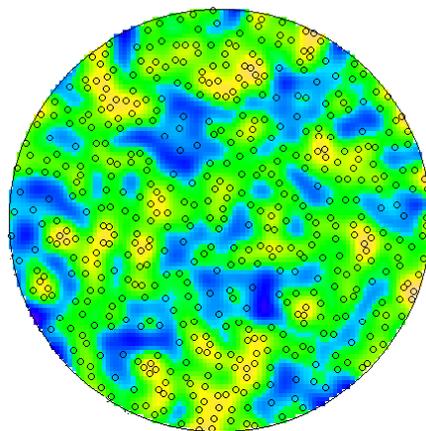
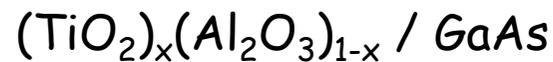
\* In collaboration with Tyndall National Institute, Ireland

# Failure events in high-K/III-V structures\*



High intensity at the edges

In case of clear nonuniformities a zoomed approach is performed:



\* In collaboration with Indian Institute of Technology, India

- Spatial statistics is a useful technique to investigate the dielectric breakdown phenomenon in MOS/MIM structures
- Caution should be exercised in reliability analysis when projecting in area failure data. This cannot be taken for granted.
- More generally, the methods described here can be easily applied to other systems exhibiting some kind of random spatial pattern
- Spatstat package for R language (freely available )



**Thank you for your attention!**

**In case of any doubt you can contact me at:  
[enrique.miranda@uab.cat](mailto:enrique.miranda@uab.cat)**

## BIO

Enrique MIRANDA was born in Buenos Aires, Argentina in 1963. He has a PhD in Electronics Engineering from the Universitat Autònoma de Barcelona (UAB), Spain (1999) and a PhD in Physics from the Universidad de Buenos Aires (UBA), Argentina (2001). From 1987 to 2003, he was Assistant Professor at the Faculty of Engineering - UBA and from 2001 to 2003, Associated Researcher of the National Council of Science and Technology-CONICET, Argentina. Since 2003, he is Professor at the Escola d'Enginyeria-UAB. Dr. Miranda has received research fellowships from the Spanish International Cooperation Agency-AECI: INTERCAMPUS (Universidad de Zaragoza) and MUTIS (UAB), from the German Exchange Academic Agency-DAAD (Technical University Hamburg-Harburg), from the Italian government (Universita degli Studi di Padova), from the Ministerio de Ciencia y Tecnología, Spain: RAMON y CAJAL (UAB), from the Matsumae International Foundation: MATSUMAE (Tokyo Institute of Technology, Japan), TAN CHIN TUAN (Nanyang Technological University, Singapore) and from the Science Foundation Ireland: WALTON visitor awards (Tyndall Institute, Ireland). He has authored and co-authored around 90 papers most of them devoted to the electron transport problem through the gate insulator in MOS devices: direct and Fowler-Nordheim tunneling, effects of trapped charge, stress-induced leakage current and post-breakdown conduction. Dr. Miranda serves as member of the Distinguished Lecturer program of the Electron Devices Society (EDS-IEEE) and is reviewer of IEEE TED, IEEE EDL, JAP, APL, TSF, MJ and MR. He also serves as Editorial Advisor of the journal Microelectronics Reliability and forms part of INFOS, IRPS, ESREF, MIEL and EMRS Technical Committees. Dr. Miranda is Visiting Scientist (2009-2012) at the National Commission of Atomic Energy (CNEA), Argentina financially supported by the Abdus Salam International Centre for Theoretical Physics, Italy.

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